

Examination in the School of Mathematical Sciences
Semester 1, 2005

3098	Communications Network Design APP MATH 4012
-------------	--------------------------------------------------------------

Official Reading Time: 10 mins
Writing Time: 180 mins
Total Duration: 190 mins

ANSWER ALL QUESTIONS
NUMBER OF QUESTIONS: 4 TOTAL MARKS: 100

Instructions

- **Answer all 4 questions**
- Begin each answer on a new page.
- Examination materials must not be removed from the examination room.

Materials

- 1 Blue book is provided.
- Calculators are not permitted.

DO NOT COMMENCE WRITING UNTIL INSTRUCTED TO DO SO.

1. Internet architectural principles:

- (a) Answer each of the following True or False
 - (i) IP is a data-link layer protocol.
 - (ii) The Internet Protocol limits the type of topology on which it can be applied.
 - (iii) In a layered model functionality is always placed exclusively at one layer.
 - (iv) a linear cost model is an ideal model for real network costs.
 - (v) a linear cost model can incorporate distance, and bandwidth related costs.
- (b) Answer each of the following in a sentence or two:
 - (i) What is the difference between the data-link layer and the physical layer of the OSI protocol stack?
 - (ii) Why is a distributed network often considered superior to a centralized network?
 - (iii) State the “robustness principle” which is often used in network design.
 - (iv) What is the key difference between packet switching and circuit switching.
 - (v) What type of measurements are needed for most network design algorithms (I do not consider cost to be a measurement).
- (c) Write a paragraph (no more than half a page) on **one** of the following topics
 - (i) The end-to-end principle
 - (ii) The impact of Moore’s law (and related laws) on the development of communications network design.

These will be assessed 50% on clarity of presentation, and 50% on content.

[25 marks]

2. Routing:

- (a) Perform Dijkstra’s algorithm on the graph shown in Figure 1 to find the shortest paths from node 1 to all other nodes. **Show your working.**

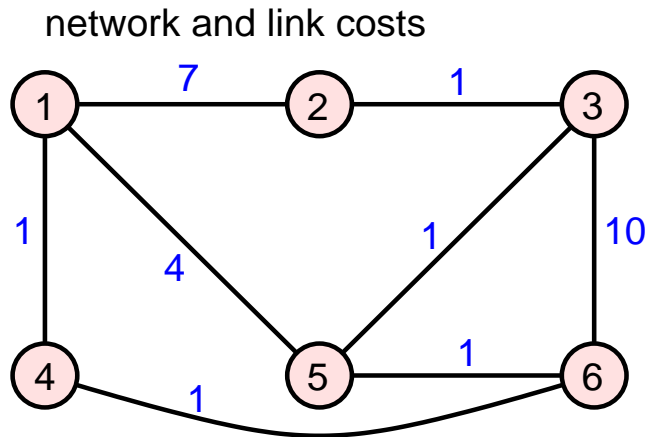


Figure 1: A network, and link costs.

- (b) Answer the following.
 - (i) State the mathematical formulation of the routing problem, with linear, separable costs. Define all of the terms used in your formulation.
 - (ii) Why does this formulation result in shortest-path routing?
 - (iii) How is Dijkstra’s algorithm applied in real network settings in order to compute shortest paths?
- (c) Name at least 5 ways in which the routing protocol BGP differs from a protocol like OSPF. Describe each of your 5 points with a couple of sentences.

[25 marks]

3. Network design

(a) Suggest three optimization *strategies* used for designing a minimum cost network. **Note:**

- I don't want an individual method, I want the underlying principle of the methods.
- I don't want a problem description either.

For each approach, provide an example of a method that applies the strategy. Very briefly outline the advantages and disadvantages of each strategy and thereby compare the three.

(b) Given a standard linear separable cost function $C(\mathbf{f}) = \sum_{e \in E} \alpha_e f_e + \beta_e$, and costs shown in Figure 2, apply Minoux's method to find a minimum cost network. **Show your working.**

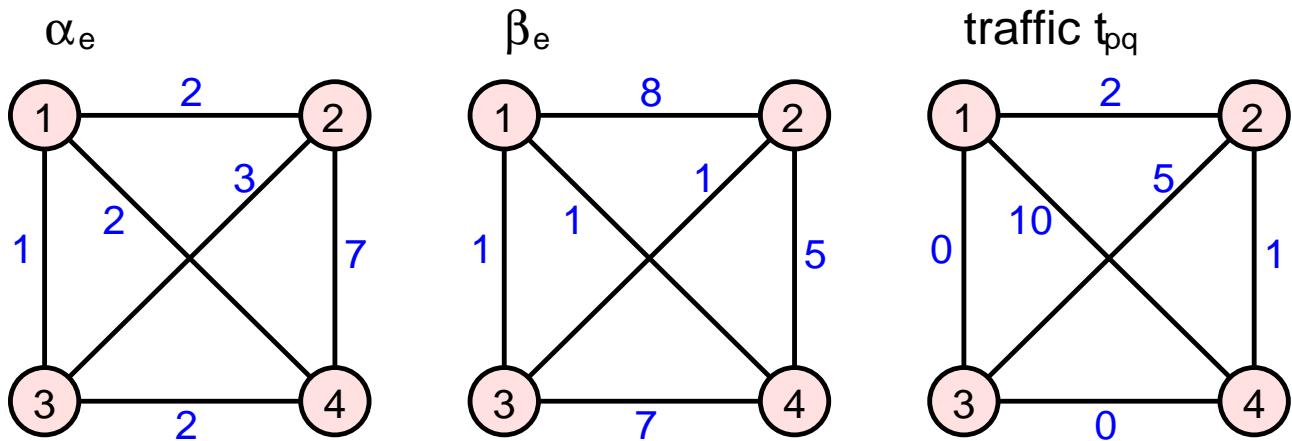


Figure 2: A network, with link costs, and offered traffic.

[25 marks]

4. Tree-like networks:

- (a) (i) Given a network, with costs $\alpha_e = 0$ and β_e given by the link attributes in Figure 3, find a minimum weight spanning tree using Prim's algorithm. **Show your working.**

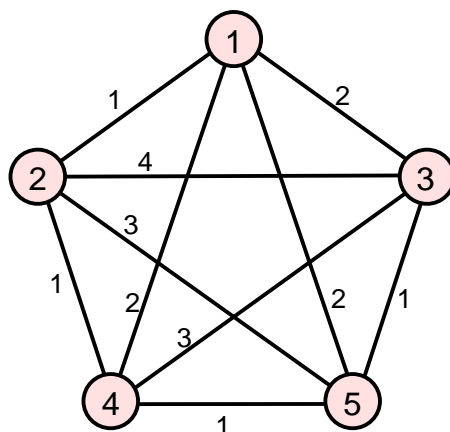


Figure 3: A network of five nodes.

- (ii) Using your minimum weight spanning tree, solve the Travelling Salesman Problem for the network to find a tour. Is it always possible to use the same approach to solving the Travelling Salesman Problem?
- (b) Provide a precise definition of
- (i) a cutset;
 - (ii) a pair of non-crossing cutsets;
 - (iii) a fundamental cutset.
- (c) Imagine a slightly different tree-like network design problem, where the $\alpha_e = 1$, and $\beta_e = 0$ for the network, and the attributes on the links in Figure 3 instead show the offered traffic between nodes (e.g. the offered traffic between nodes 2 and 3 is 4).
- (i) Given the following minimal cutsets for the first 3 iterations of Gusfield's algorithm, show the network at each step.

iteration	X for the minimal cutset
step 1	{2, 3, 4, 5}
step 2	{3, 1, 4, 5}
step 3	{4}

- (ii) Perform the complete **last step** of Gusfield's algorithm to find the minimum spanning tree for the network. **Show your working.**
- (iii) Compare your result above with the result from a minimal star design (given the same cost function). Note this is different from a minimum distance star.

[25 marks]