

# Statistically Accurate Network Measurements

Matthew Roughan

<matthew.roughan@adelaide.edu.au>

with Hung Nguyen

Applied Mathematics

School of Mathematical Sciences

University of Adelaide

June 4, 2010

# Network Measurements

"Measure what is measurable, and make measurable what is not so."

Galileo Galilei, (1564 - 1642)

"To measure is to know."

Lord Kelvin, Sir William Thomson (1824-1907)

# The problem

---

- Computer science
  - we deal with digital data
  - there is a tendency to believe we see reality
- Measurements are **ALWAYS** flawed
  - measurement precision
  - ambiguity
  - missing data
  - measurement artifacts
  - impact of the measurements themselves
- So what do I do?
  - make more measurements
  - do a bit of stats ...

# So What?

---

Statistics has been solving these sorts of problems for a while.

- Why isn't this all easy?

# So What?

---

Statistics has been solving these sorts of problems for a while.

- Why isn't this all easy?
- I'm a bit clueless

# So What?

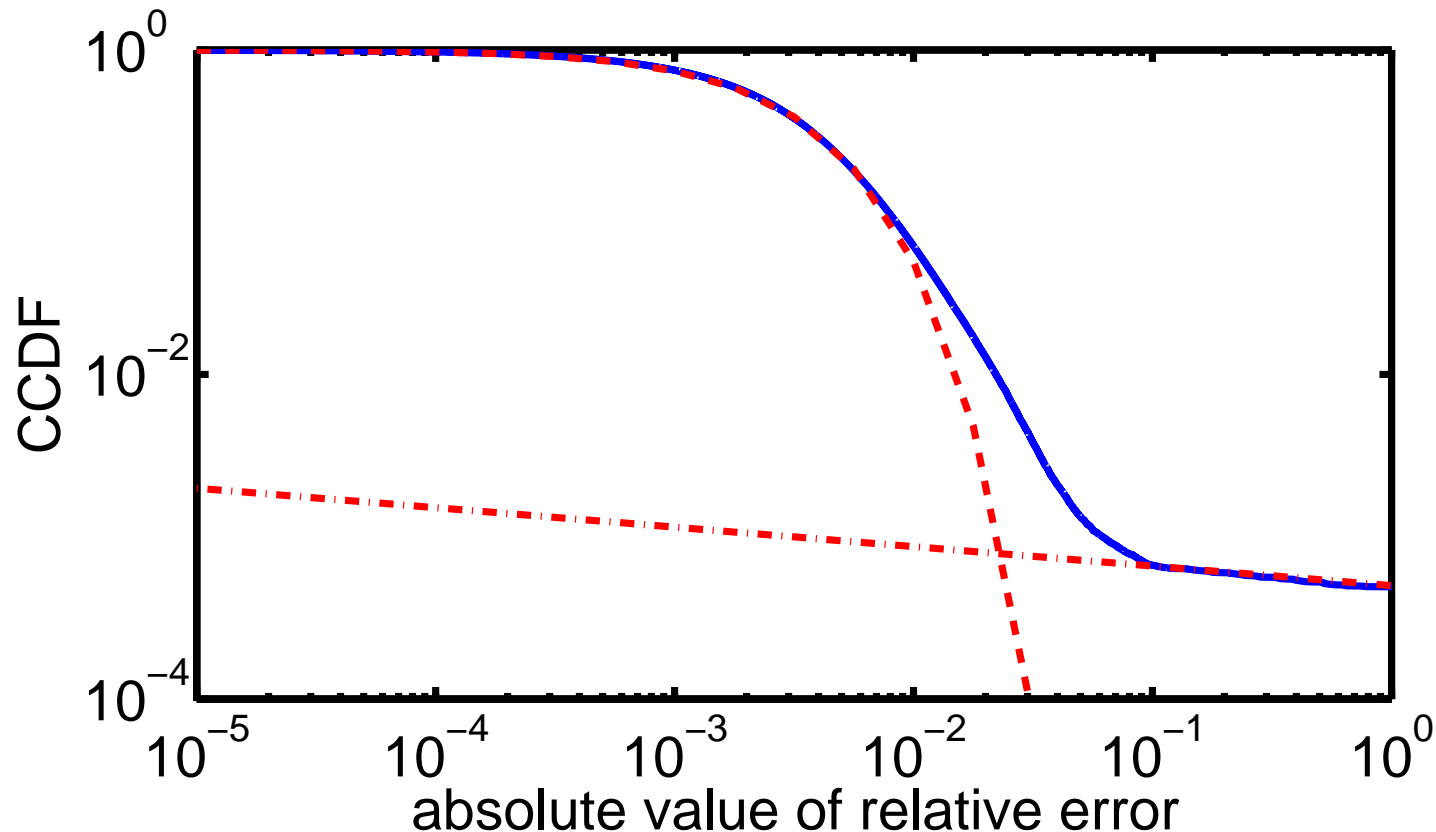
---

Statistics has been solving these sorts of problems for a while.

- Why isn't this all easy?
- I'm a bit clueless
- There are some hard bits
  - non-Gaussian distributions and heavy-tails
  - strong correlations (and long-range dependence)
  - structural biases in sampling
  - we don't get to see what we would like to see

# Examples: Traffic

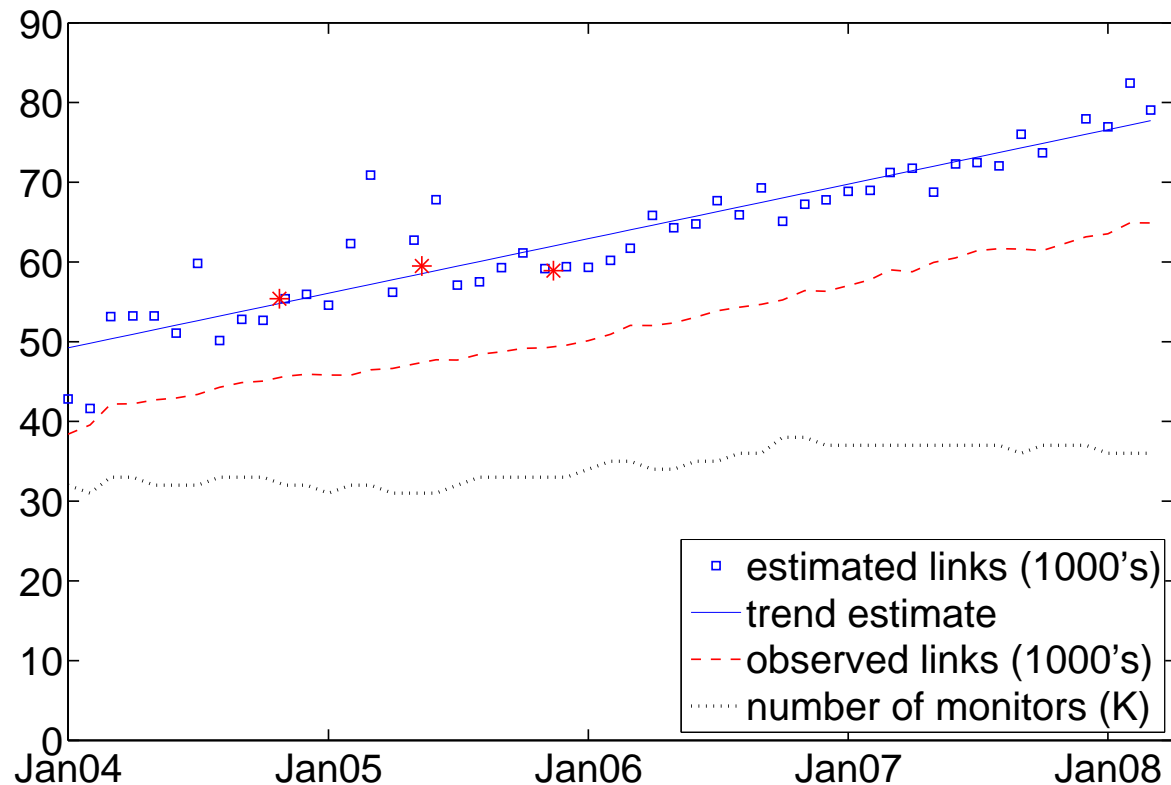
- estimating traffic matrices from link data [1, 2, 3, 4]
- interpolating missing data in traffic matrices [5]
- SNMP link measurement errors [6]



# Examples: Routing and Topology

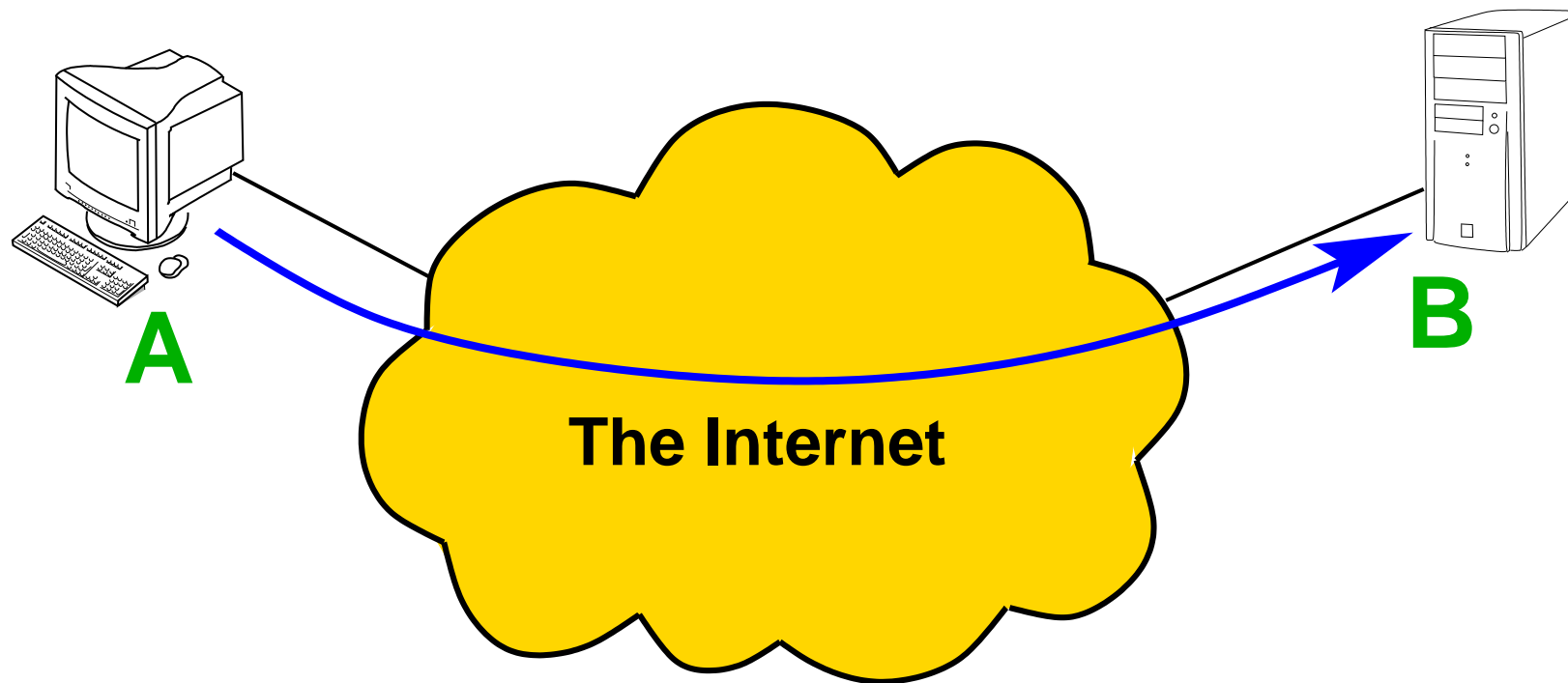


- traceroute aliasing problem [7]
- load-balancing [8]
- bias in sampled viewpoint [9, 10, 11]



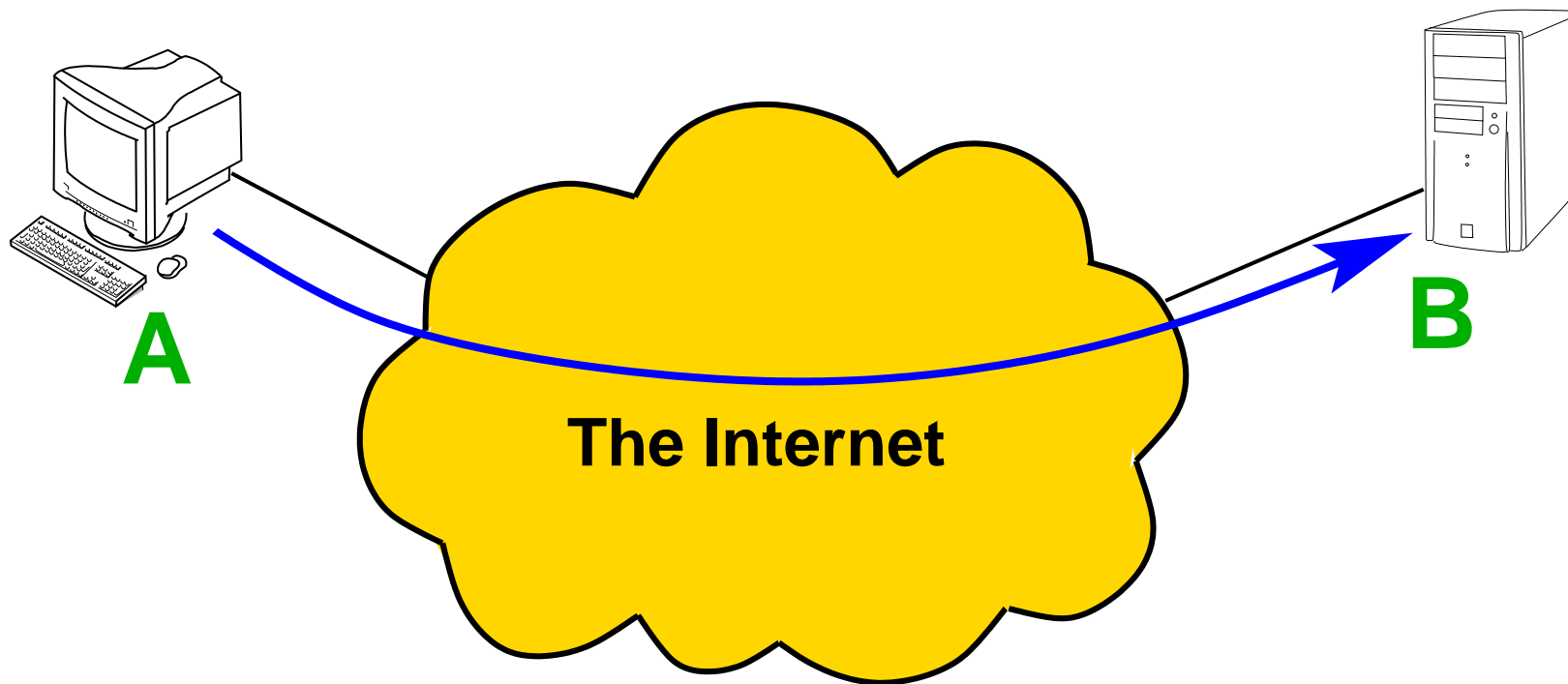
# Examples: Performance

- Active performance measurements
- Send probe packets from  $A \rightarrow B$  across the network
- Measure the performance experienced by packets



# The problem

- How accurate are the probes?
- How many probes should we send?
- When is there a network problem?



# Accuracy

What do we mean by accuracy?

- probes are samples from some underlying process
  - assume measurement equipment has no flaws
- measurements over time can be averaged to give estimates
- implicit assumption of stationary ergodic process
  - ⇒ a time average converges to an ensemble average
- variance can be estimated
  - typically under the assumption of independent measurements

Accuracy of **estimates** not individual measurements

# The plural of ...

---

"The plural of anecdote is not evidence."  
Alan L. Leshner

# The plural of ...

"The plural of anecdote is not evidence."  
Alan L. Leshner

A Unicorn



If you Google "Unicorn", you'll get about 3 million images, mostly resembling this.

# The plural of ...

"The plural of anecdote is not evidence."  
Alan L. Leshner

A Rhino



Unicorn images aren't too evocative of the Rhinoceros

# The plural of ...

"The plural of anecdote is not evidence."  
Alan L. Leshner

A NarWhal



Throw in some narwhal horns for confusion

# Correlated Measurements

The underlying problem is that correlated measurements don't give you extra information in the same way independent measurements do.

- if the measurements are really from the same source (e.g. Unicorn myths) then they give you no extra information
- what about packet probes?
  - are they correlated?

# Answers

- Yes!
  - there are correlations in measurements, e.g., [12, 13, 14, 15]
  - the short-range correlations can be quite strong even where there is no long-range dependence.
  - these correlations must be taken into account in estimating accuracy, confidence intervals, ...
- correlations get stronger the closer measurements are in time [16]
  - within a finite sampling period there is no point in arbitrarily increasing the number of samples
- correlations are load dependent [16]

# Consider loss measurements

- Used for
  - alarms - signal network problems
  - Service-Level Agreement (SLA) compliance
- typical approach:
  - assume Bernoulli (independent) trials
  - but its well known there are correlations
- Why do we care about accuracy
  - are we compliant with an SLA
  - if "accuracy" of measurements is wrong, we may mistakenly claim compliance, or otherwise

# Loss measurement estimation

Standard estimator of loss probability

$$\hat{p} = \frac{1}{N} \sum_{i=1}^N I_i, \quad (0)$$

where  $I_i = 1$  if probe  $i$ th is lost, and  $I_i = 0$  otherwise, and

$$\text{Var}[\hat{p}] = \frac{1}{N^2} \sum_{i=1}^N \sum_{j=1}^N R(\tau_{ij}),$$

- $R(\tau)$  is the autocovariance of the loss process.
- $\tau_{ij}$  is the time between the  $i$  and  $j$ th probes.

# Possible Approaches

- Assume independence

$$\text{Var} [\hat{p}] = p(1 - p)/N,$$

- Estimate  $R_{ij}$ :
  - treat measurements like a discrete process
  - but then we are limited to those measurements
  - better to estimate underlying process
- Estimate  $R(\cdot)$  directly from data
  - estimates of  $R(\cdot)$  have a high variance themselves
- **Estimate  $R(\cdot)$  with the help of a model**

# Our Approach

---

- Model + parametric estimation
  - model simple enough to work with
  - general enough to fit data
  - model underlying loss, not packet losses
- Markov model doesn't work too well
  - need too many states
- Alternating renewal model is attractive
  - approximately matches data
  - fits our intuition about loss bursts
    - from queueing
    - from routing events

# Alternating Renewal Model

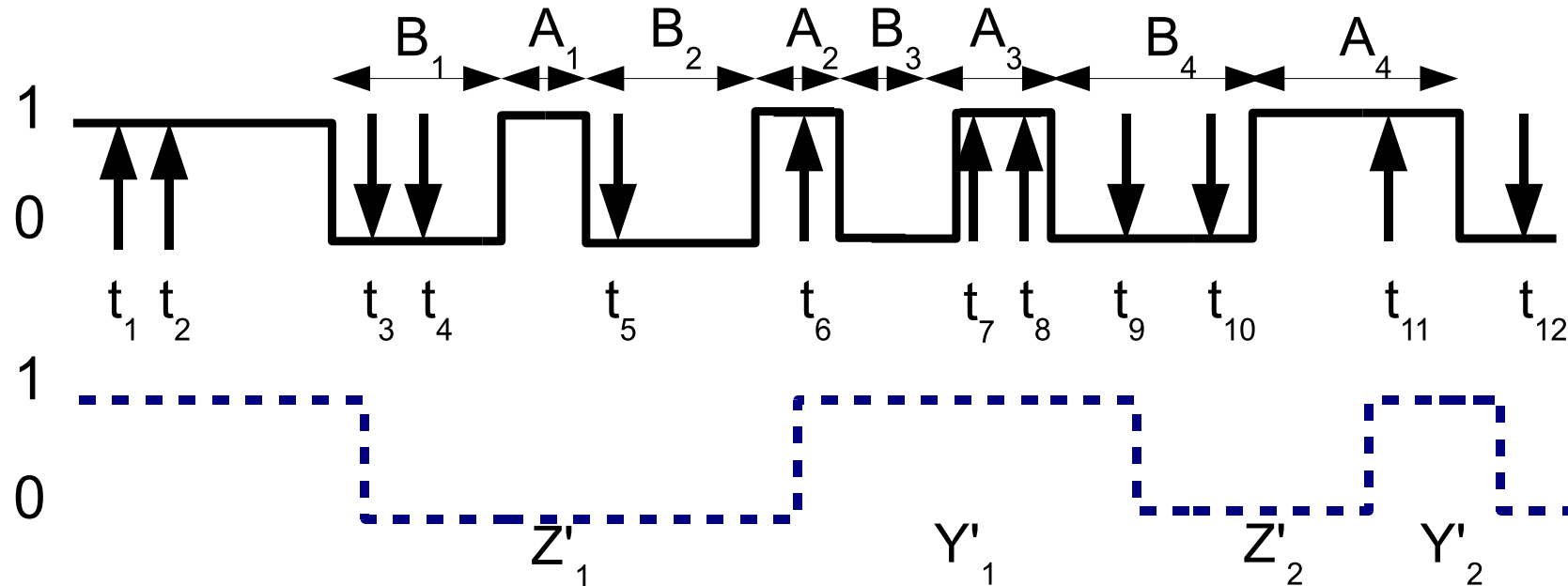


- On/Off process
  - On and Off times are independent
  - On times form IID sequence
  - Off times form IID sequence
- Parameterise the distribution of On/Off times
  - we used Gamma distribution
  - natural generalization of the exponential

$$\text{Prob}\{X \in [x, x + dx)\} = x^{k-1} \frac{e^{-x/\theta}}{\Gamma(k)\theta^k} dx,$$

- two parameters
  - shape  $k$  ( $k = 1$  gives exponential distribution)
  - scale  $\theta$

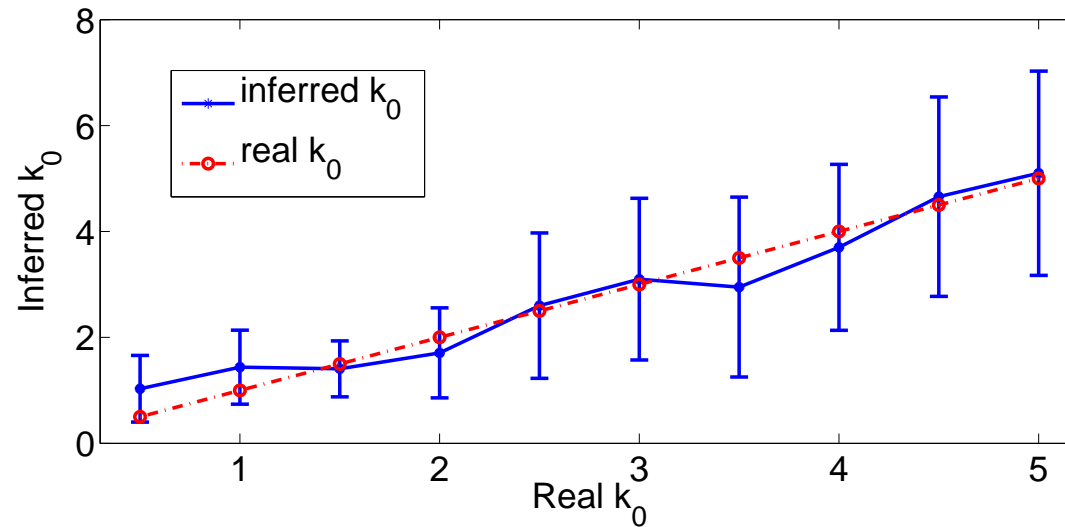
## Samples from underlying loss-process



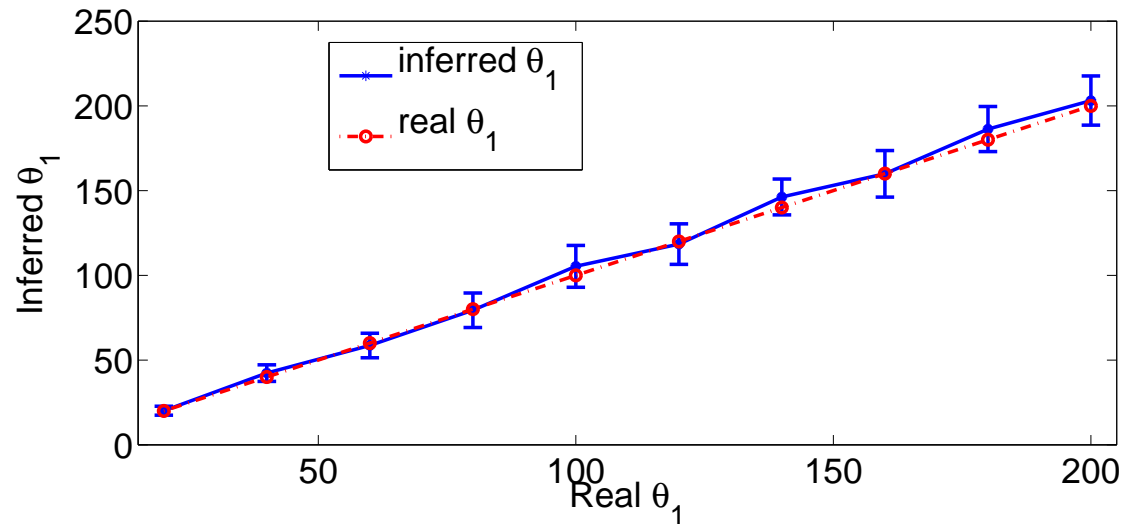
- samples can miss some intervals
- direct estimation of intervals overestimates them
- estimation using Hidden Semi-Markov Model techniques

# Simulations: test estimates

Varying  $k_0$ ,  $\lambda=0.1$ ,  $k_1=5$ ,  $\theta_0=10$ ,  $\theta_1=100$



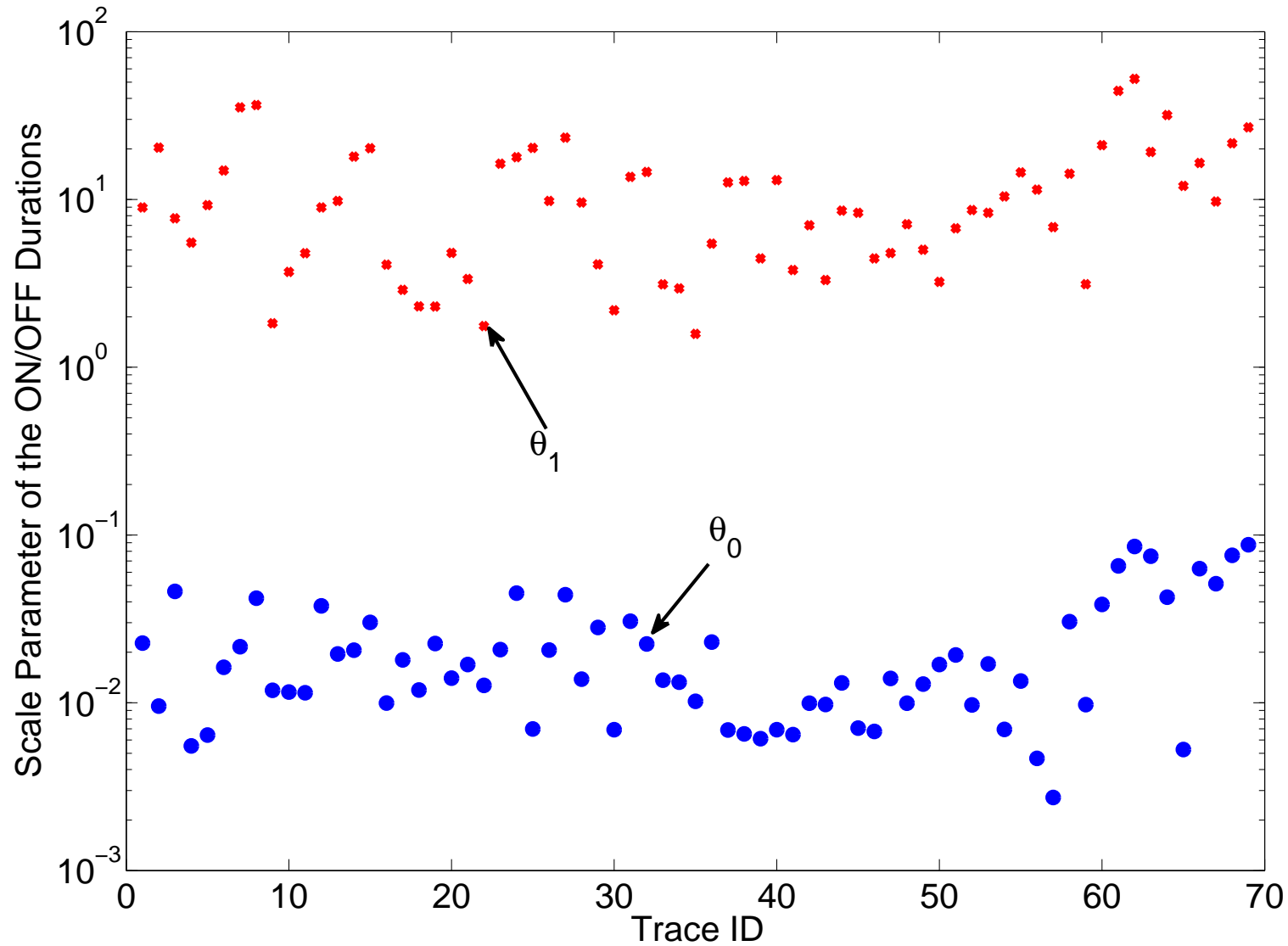
Varying  $\theta_1$ ,  $\lambda=0.1$ ,  $k_0=1$ ,  $k_1=5$ ,  $\theta_0=10$



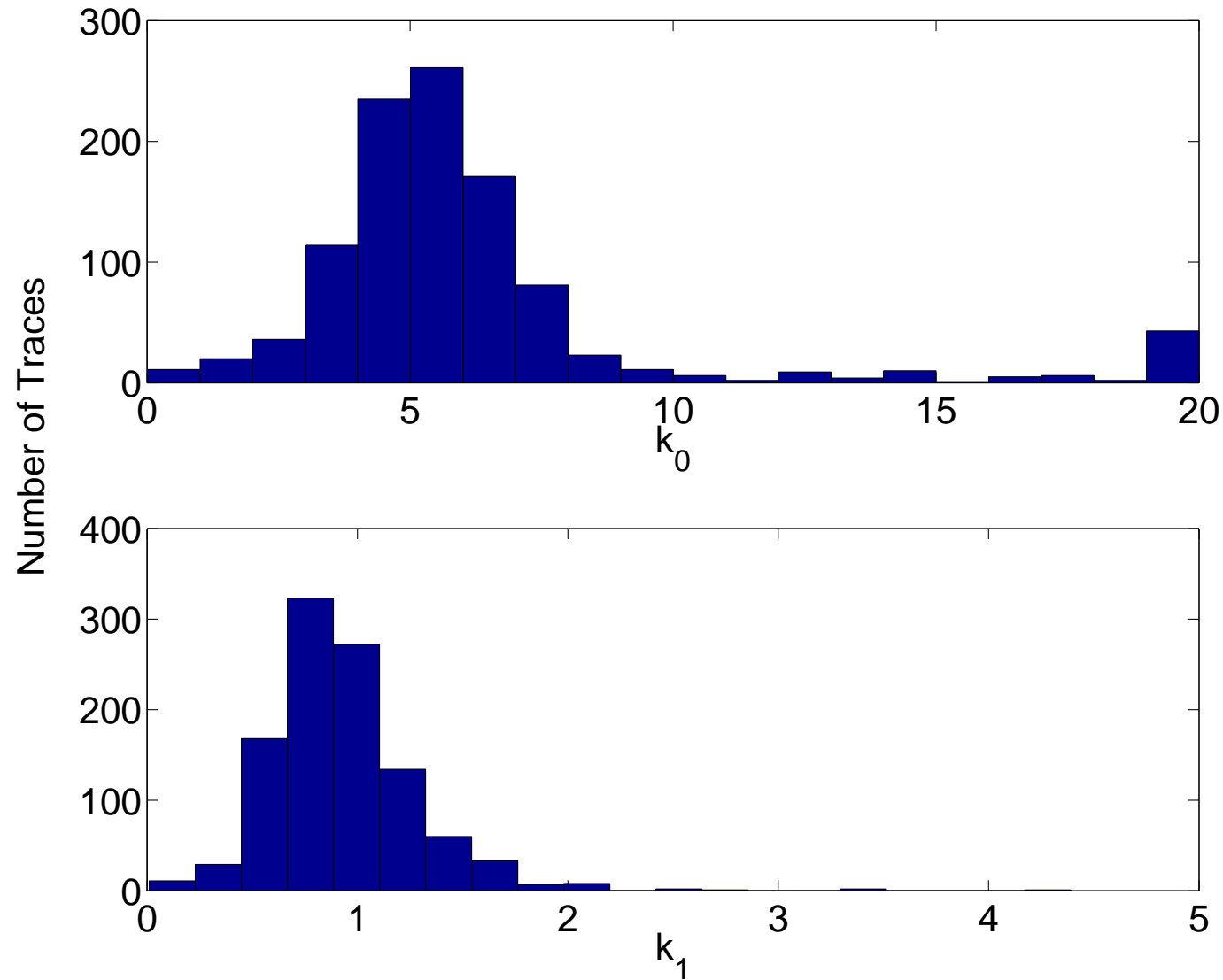
# Experiments

- Measurement locations
  - One way Planetlab → Planetlab
  - Between dedicated machines
    - EPFL and Australia
  - Web server probes
  - DNS server probes (provided by QUEEN)
- Standard Traces
  - 10,000 40 byte UDP probe packets
  - Sent as Poisson process average rate 10 packets per second
  - Filtered for stationarity and non-negligible loss
  - 1,100 traces analysed

# Results: $\theta$



# Results: $k$

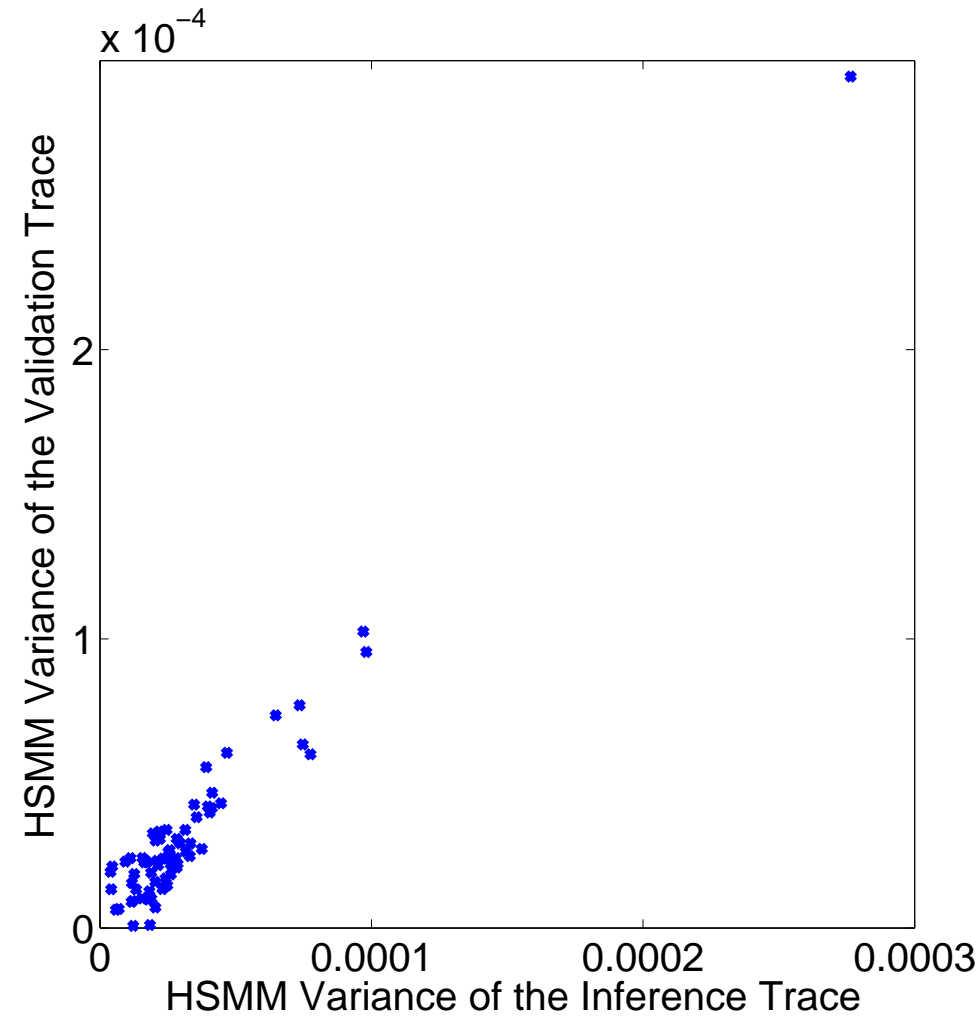
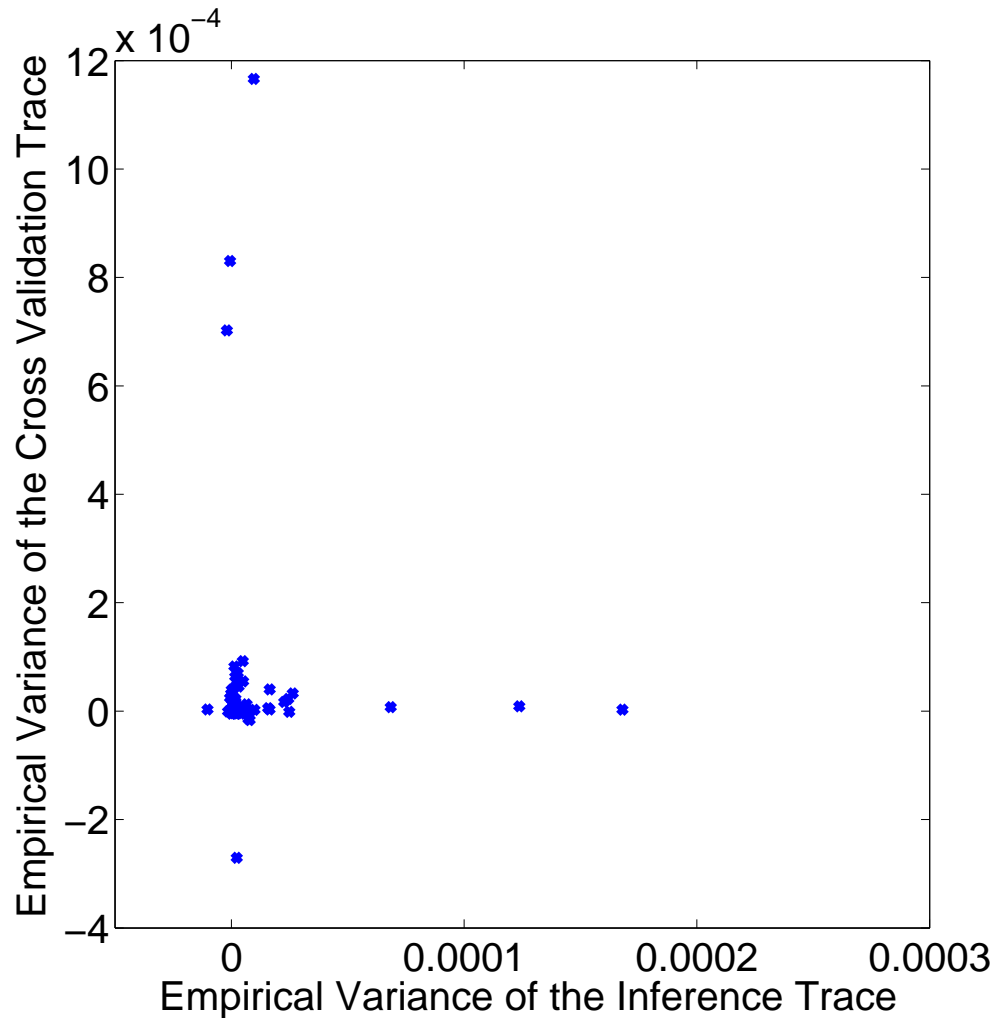


# Validation

---

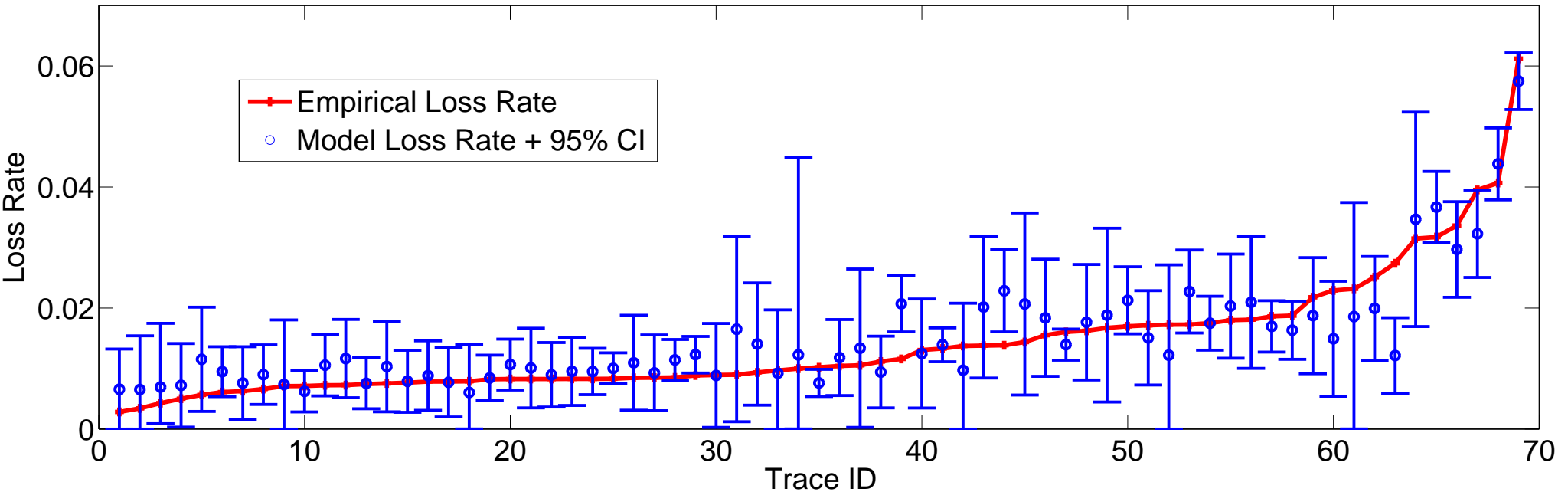
- Hard to get ground truth to compare against
- test by sub-sampling
  - randomly segregate data into two sections
    - each is still Poisson probe process
  - compute results for both
  - look for consistency

# Validation: consistency variance



# Validation: confidence intervals

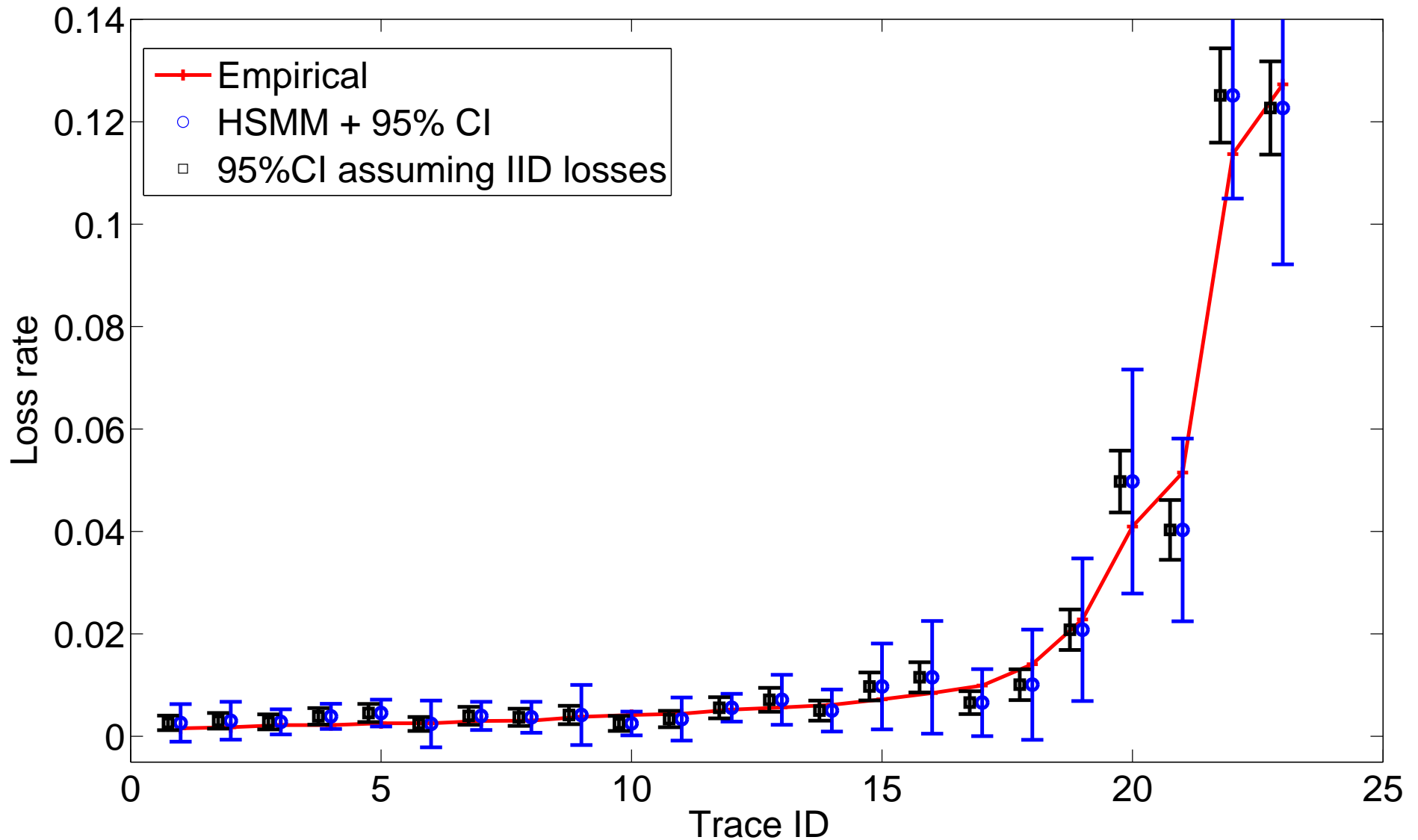
Cross Validation of the SAIL algorithm



- 95th percentile confidence intervals match in 92% of 1,100 traces
  - independent CIs given 63% coverage
- width of CIs is LARGE

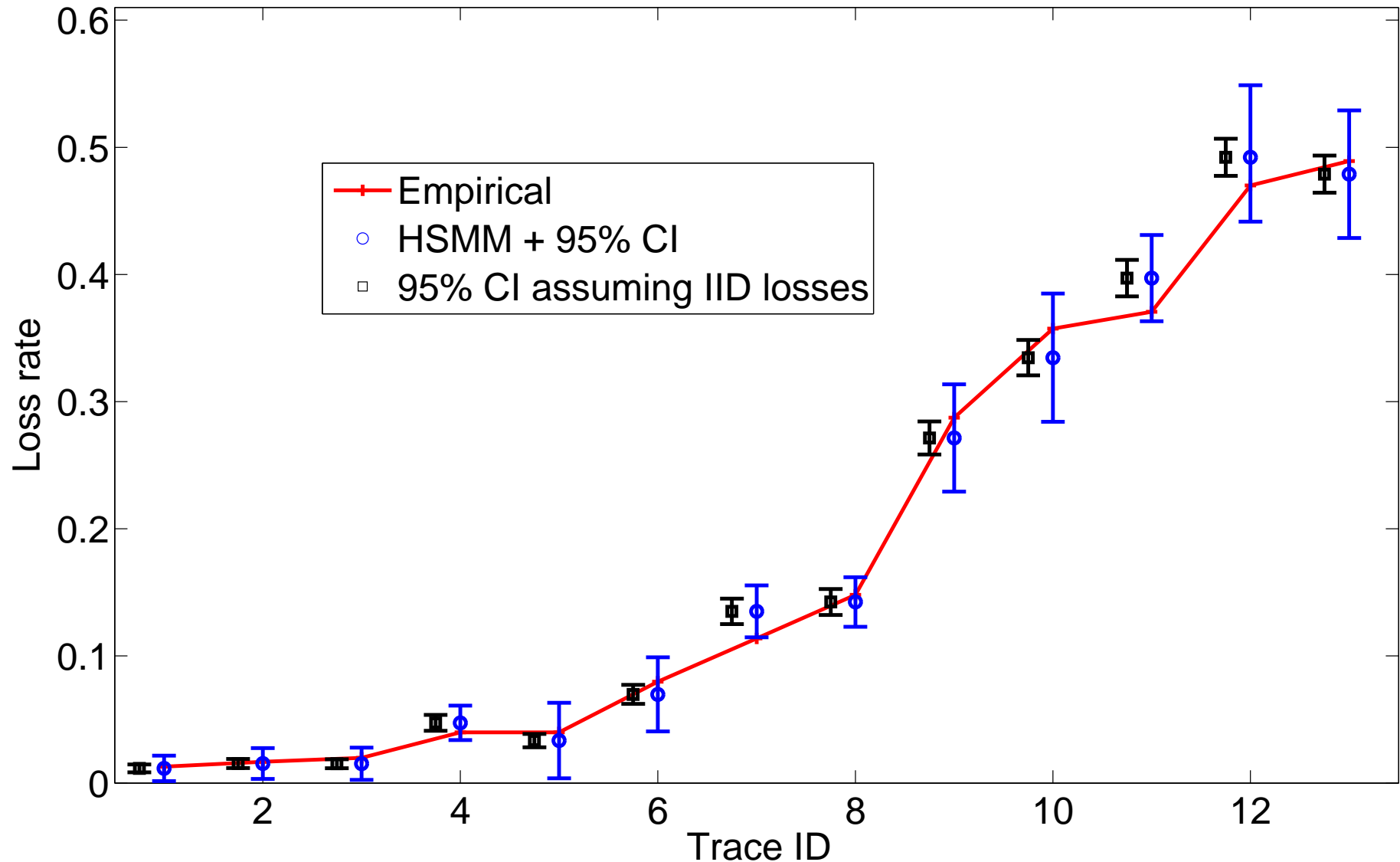
# Validation: Web data

Web server losses



# Validation: DNS data

DNS server losses (Queen's data)



# Conclusion

---

- Measurements needs stats
  - How do you know when a measurement is any good otherwise?
  - Need to deal with all the difficulties of Internet
    - e.g., correlations
- What if I measure every packet?
  - measurements today are for prediction tomorrow
- Loss measurements in particular
  - we have a working technique for loss measurements that copes with the correlations
- Full technical report, data and code are available at <http://www.adelaide.edu.au/directory/hung.nguyen>.

# Accuracy

What do we mean by accuracy?

- probes are samples from some underlying process
  - assume measurement equipment has no flaws
- measurements over time can be averaged to give estimates
- implicit assumption of stationary ergodic process  
⇒ a time average converges to an ensemble average
- variance can be estimated by the  
**Central Limit Theorem**

Accuracy of **estimates** not individual measurements

## Central Limit Theorem

For a set of independent, identically distributed RVs  $X_i$ , the sample mean

$$\hat{X} = \frac{1}{N} \sum_{i=1}^N X_i,$$

has expectation  $E[\hat{X}] = E[X_1]$ , and as  $N \rightarrow \infty$

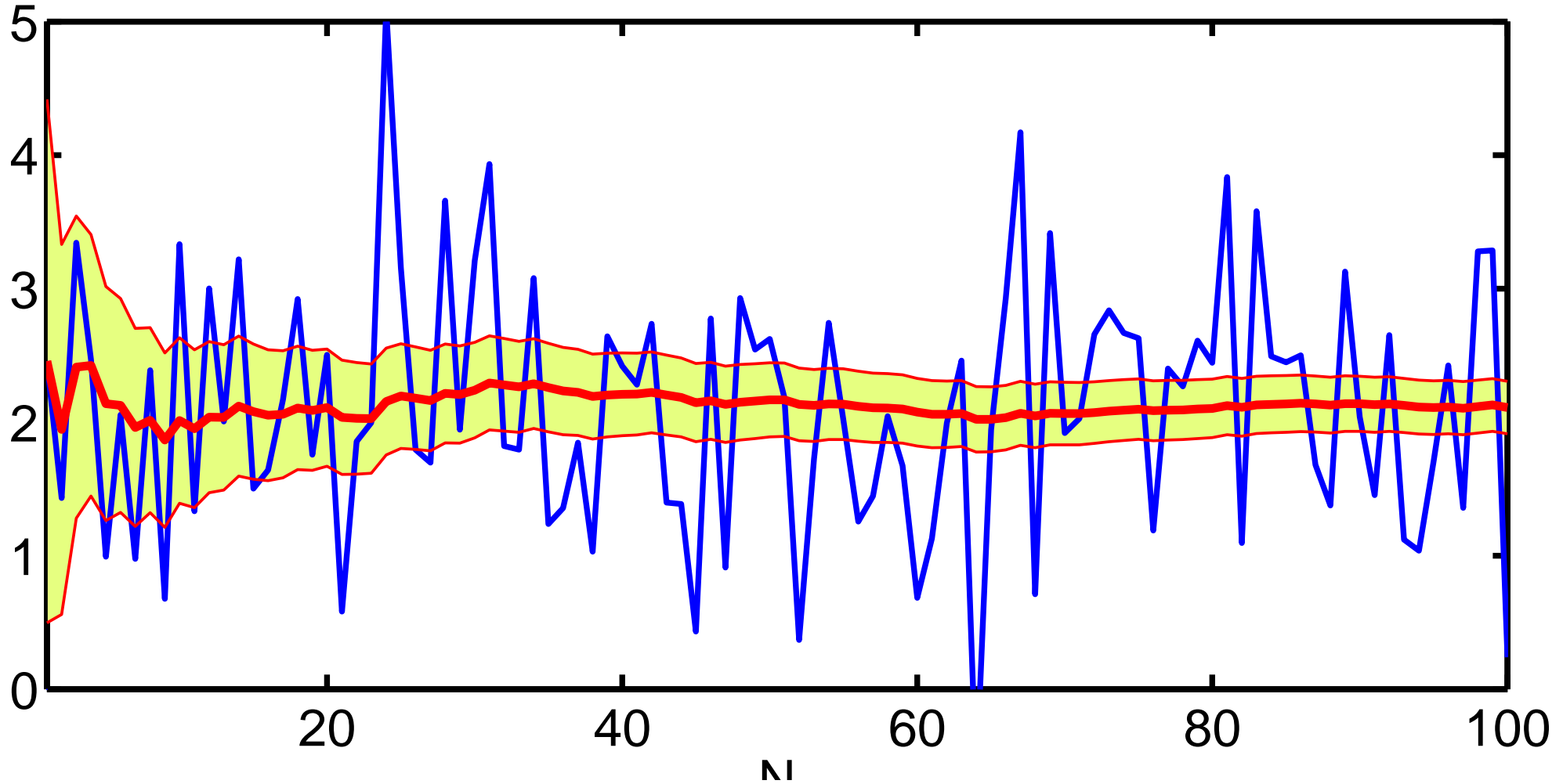
$$\sqrt{N} (\hat{X} - E[X_1]) \rightarrow N(0, \sigma^2)$$

in distribution, where  $\sigma^2 = \text{Var}[X_1]$ .

So the 95th% CIs of estimate  $\hat{X}$  are  $\pm 1.96\sigma/\sqrt{N}$ .

# Example

White noise



# CLT: continuous time

Continuous time process  $X(t)$  where the sample mean

$$\hat{X} = \frac{1}{T} \int_0^T X(u) du$$

converges to the true mean  $\hat{X} \rightarrow E[X]$ , and

$$\sqrt{T} (\hat{X} - E[X]) \rightarrow N(0, s^2)$$

in distribution as  $T \rightarrow \infty$ , where

$$s^2 = 2\sigma^2 \int_0^\infty r(u) du$$

where  $\sigma^2 = \text{Var}[X]$ , and  $r(s)$  is the autocorrelation of  $X(t)$ .

# Discrete samples

- Correlations are not only a continuous time problem
- Discrete (uniform) samples (interval  $\delta t$ )

$$s^2 = \sigma^2 \left[ 1 + 2 \sum_{i=1}^{\infty} r(k \delta t) \right]$$

- Poisson samples (rate  $\lambda$ )

$$s^2 = \sigma^2 \left[ \frac{1}{\lambda} + 2 \int_0^{\infty} r(u) du \right]$$

# A simple example: the M/M/1 queue



- Poisson packet arrivals (rate  $\lambda$ )
- Exponential service times (mean  $1/\mu$ )
- $Q$  = number in system (for  $\rho = \lambda/\mu$ )

$$E[Q] = \frac{\rho}{1-\rho} \quad \text{and} \quad \text{Var}[Q] = \frac{\rho}{(1-\rho)^2}$$

- Autocorrelation (Whitt 1989 [17], Morse 1955 [18])

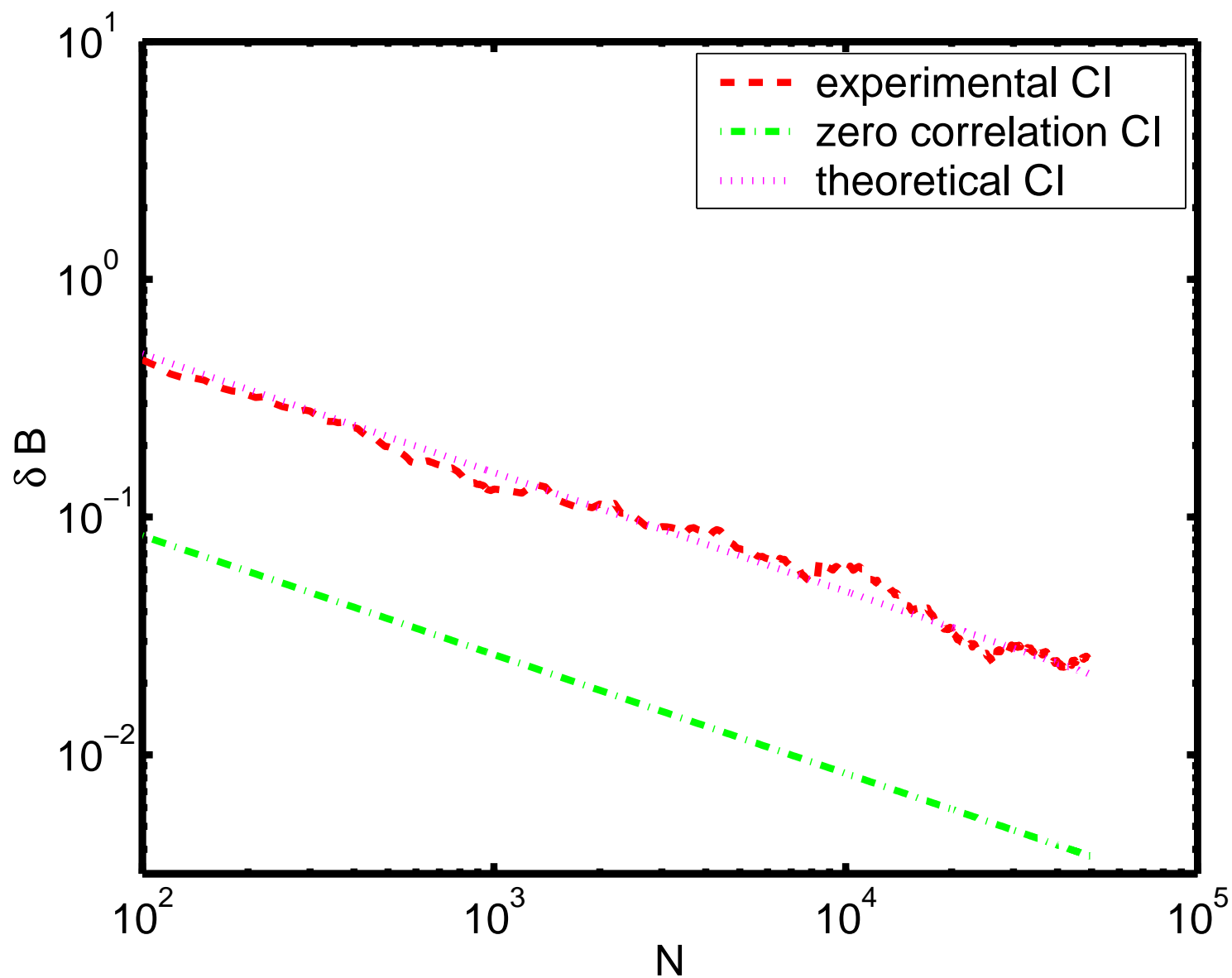
$$r(t) = \frac{\lambda^2}{(\mu - \lambda)^2} + (\mu - \lambda) \frac{\lambda\mu}{\pi} \int_0^{2\pi} \frac{\sin^2 \theta e^{-t(\mu + \lambda - 2\sqrt{\lambda\mu} \cos \theta)}}{(\mu + \lambda - 2\sqrt{\lambda\mu} \cos \theta)^3} d\theta$$

- asymptotic variance for M/M/1 (Whitt 1989)

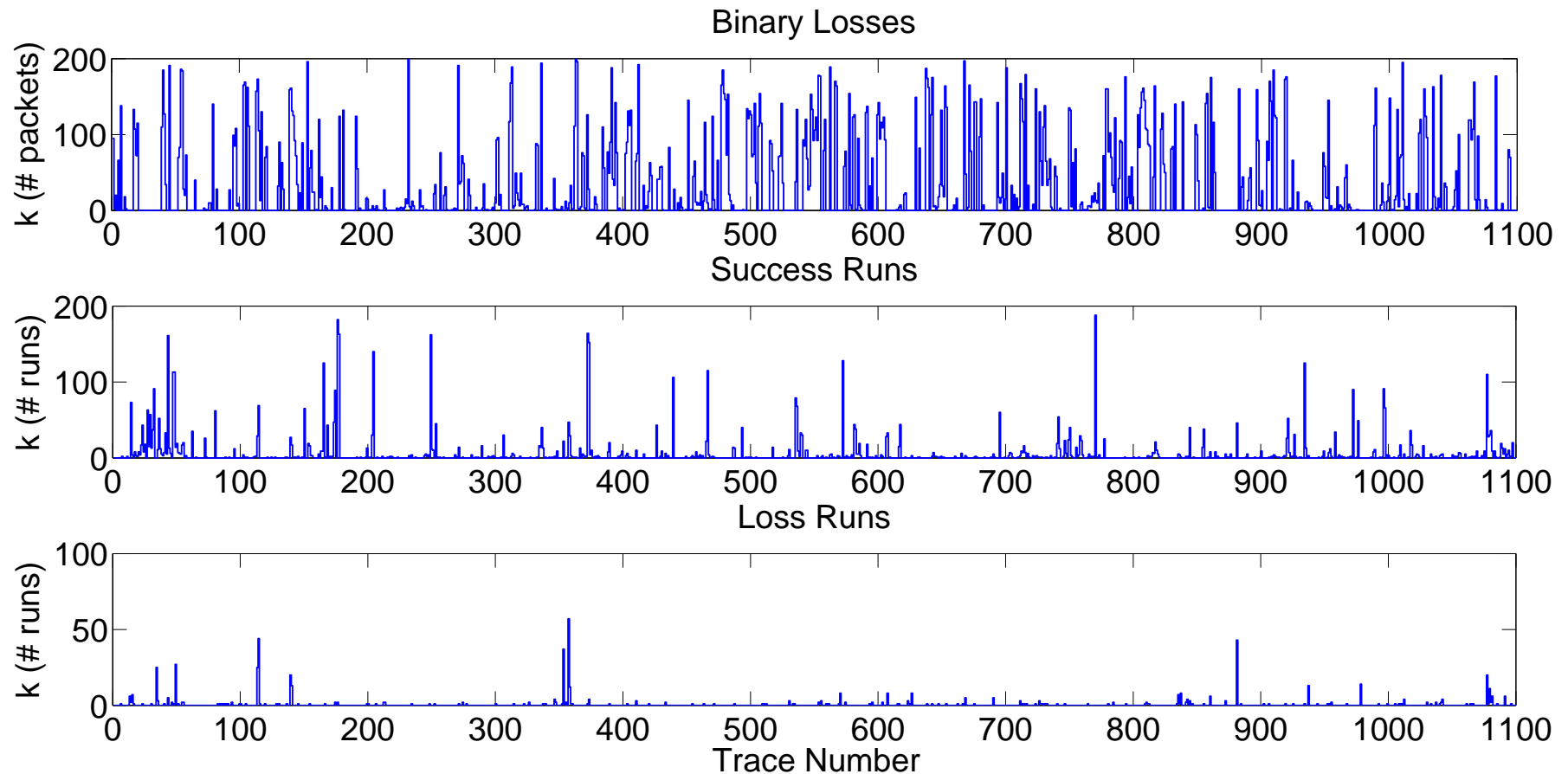
$$s^2 \simeq \frac{4\rho^2}{(1-\rho)^4}$$

# Results M/M/1

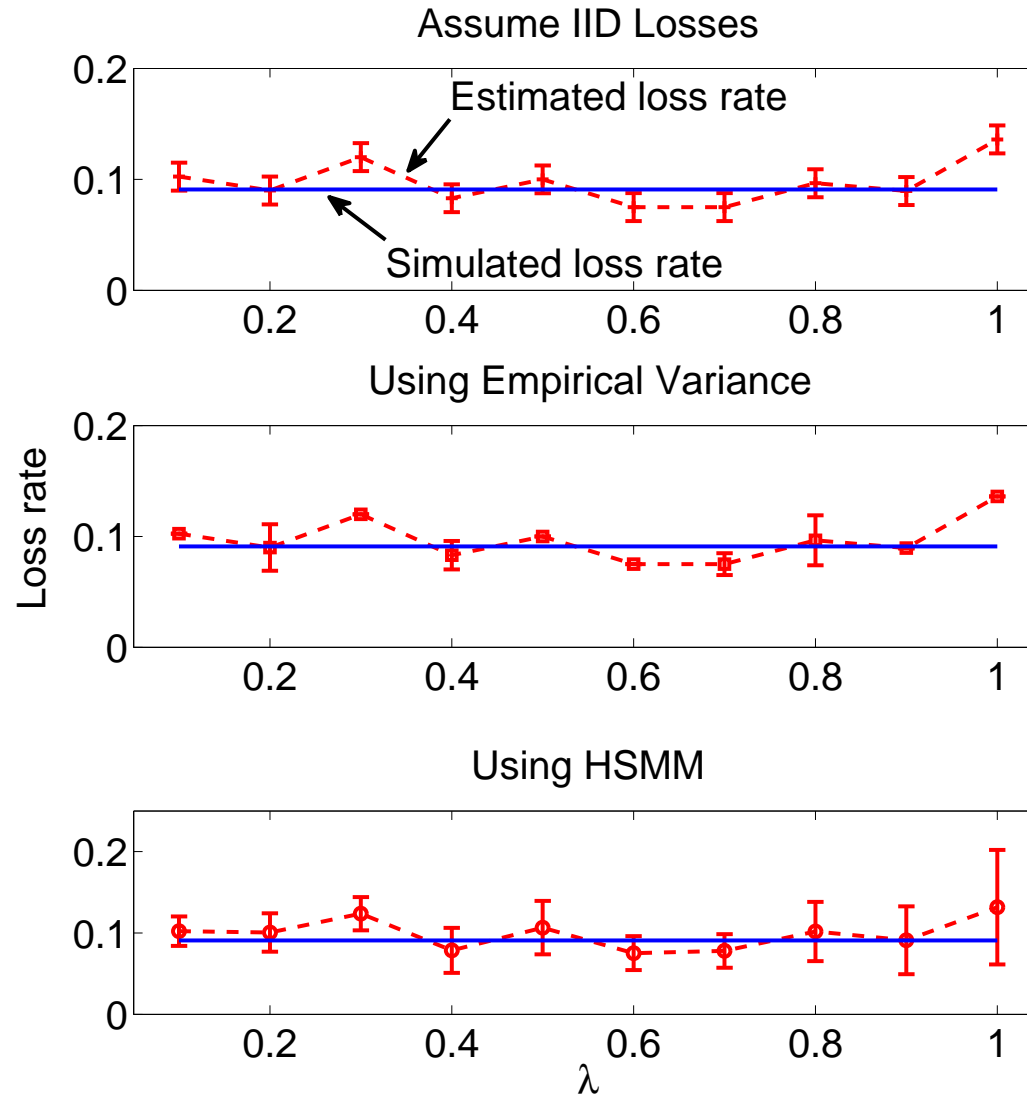
$\rho = 0.7$



## Validity of Semi-Markov Model



# Simulations: comparisons



# References

- [1] Y. Vardi, "Network tomography," *Journal of the American Statistical Association*, March 1996.
- [2] Y. Zhang, M. Roughan, N. Duffield, and A. Greenberg, "Fast accurate computation of large-scale IP traffic matrices from link loads," in *ACM SIGMETRICS*, (San Diego, California), pp. 206-217, June 2003.
- [3] Y. Zhang, M. Roughan, C. Lund, and D. Donoho, "An information-theoretic approach to traffic matrix estimation," in *ACM SIGCOMM*, (Karlsruhe, Germany), pp. 301-312, August 2003.
- [4] Y. Zhang, M. Roughan, C. Lund, and D. Donoho, "Estimating point-to-point and point-to-multipoint traffic matrices: An information-theoretic approach," *IEEE/ACM Transactions on Networking*, vol. 13, pp. 947-960, October 2005.
- [5] Y. Zhang, M. Roughan, W. Willinger, and L. Qui, "Spatio-temporal compressive sensing and Internet traffic matrices," in *ACM Sigcomm*, (Barcellona, Spain), pp. 267-278, August 2009.
- [6] M. Roughan, "A case-study of the accuracy of SNMP measurements," *Journal of Electrical and Computer Engineering*, vol. 2010, 2010. Article ID 812979, doi:10.1155/2010/812979.  
<http://www.hindawi.com/journals/jece/2010/812979.html>.
- [7] L. Li, D. Alderson, W. Willinger, and J. Doyle, "A first-principles approach to understanding the internet's network structure," in *Workshop on Statistics of Networks*, June 2010 – p.38/38