

#### The Predictive Power of Shortest-Path Weight Inference

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Let's go a reverse engineering, hey!

- do a bunch of traceroutes from as many places, to as many places as possible
- compile them together
- infer
  - topology
  - routing
  - of a single AS (at a time)
- invaluable
  - scientific interest
  - for simulations

## Network Tomography



Network Tomography can be generally applied to mean solving inverse problems in communications networks.

- link performance (from end-to-end measurements)
- end-to-end traffic matrices (from link loads)
- topology
- routing

# Routing Policy Inference



- current routing is implicit in traceroute measurements
- but of limited utility
- doesn't tell you what will happen if something changes
  - thats where the money is
  - also useful for understanding the mind of the "network engineer"
- really need to infer routing policies
  - simplest case is shortest-path routing
  - infer weights



Intuition: measured paths must be shortest-paths Write as optimization problem (actually a LP)

$$\begin{array}{l} \text{minimize } f = \sum_{e \in E} \varepsilon_e, \\ \text{subject to} \\ w_e - \varepsilon_e \leq d_e, \quad \forall e \in E, \\ w_e + \varepsilon_e \geq d_e, \quad \forall e \in E, \\ \sum_{e \in \hat{\mu}_{ij}} w_e \leq \sum_{e \in \mu} w_e, \quad \forall i, j \in N, \text{ and } \forall \mu \in P_{ij}, \\ w_e, \varepsilon_e \geq 0, \quad \forall e \in E, \end{array}$$

where

 $\blacksquare$   $w_e$  are the link weights

d<sub>e</sub> are the links' geographic distances

## Rocketfuel as tomography



Rocketfuel technique is a really a type of tomography

- inverse problem
- constraints imposed by measurements
- problem is underconstrained
- Need side-information
  - often called a "prior"
  - The Rocketfuel prior is distance proportionality
    - in absence of other information, shortest-path weights should be geographic distance
    - but we know this is wrong
    - Does it work anyway?





How would we know if it worked?

"accuracy" is meaningless here





How would we know if it worked?

we can change a weight, without changing routing







How would we know if it worked?

we can change a whole lot of weights



## Predictive power



What is really interesting is how well we can predict the network behaviour

- obviously has to be behaviour that we don't "see"
  - optimization automatically ensures that weights will fit the observed routing
- two cases considered here
  - unobserved routes (incomplete data)
  - routing after a link failure

# Methodology



- Used real data (Abilene, GEANT)
  - doesn't allow for multiple simulations
  - doesn't allow us to vary real prior
- Combined with simulations
  - 1. start with a topology (real, or Rocketfuel)
  - 2. generate a set of traffic
  - 3. generate sets of weights
    - (a) Given weights (some distance proportionality)
    - (b) Unit (less distance proportionality)
    - (c) Unit plus jitter
    - (d) Optimized weights (no distance correlation)
    - (e) "Backbone" weights (spanning tree + backup) (very far from proportional)

#### Unobserved routes results



Predictive power (on average) for 5 (randomly chosen) unobserved routes

	weights					
Network	given	unit	u+j	synthetic	backbone	
AS 1	97.3%	95.3%	95.5%	92.9%	78.3%	
AS 1239	96.6%	96.4%	96.6%	92.9%	74.2%	
GEANT	91.5%	95.4%	94.4%	90.3%	67.8%	

results are reasonable to very good

real distribution of weight values plays little role, unless it is really extreme

### Link failure results



Predictive power for routing after single links failures

	weights					
Network	given	unit	u+j	synthetic	backbone	
AS 1	94.4%	99.9%	99.2%	90.9%	69.5%	
1239	89.9%	100.0%	94.1%	59.8%	27.3%	
GEANT	87.8%	99.7%	94.2%	74.7%	35.5%	

harder task

most cases perform worse than before

- now, weight distribution plays more of a role
  - weights further from distance perform worse

## Other results





#### IMC'08 – p.12/15

## Conclusion



- Rocketfuel approach isn't bad (in the absence of anything better)
- Predictive power is a useful methodology not just for this problem but for a range of inverse (tomography) problems where outright accuracy isn't really the important feature

Future work

- improved algorithms
- incorporating topology errors
- further investigation of information reversal

## ECMP



Equal-Cost Multiple Paths (ECMP) is important

- effects routing
- effects measurements
- effects inference
- effects interpretation of results

paper lists effects  $\pm$  effects of ECMP

#### **Computation Time**



1.8 Ghz Intel PC

• times are  $O(|E|^3)$ 

