# How I Learned to Stop Worrying and Love Traffic Matrices

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UoA

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#### **Acks**

Many people have helped with the work described here, here's just a few in no particular order

- Albert Greenberg
- Yin Zhang
- Paul Tune
- Walter Willinger
- Zihui Ge
- Jen Yates
- Nick Duffield
- Anja Feldman
- Carsten Lund
- David Donoho
- Mikkel Thorup

and many others.



#### Additional Information

More complete notes can be found in Internet Traffic Matrices: A
 Primer, Paul Tune and Matthew Roughan, ACM Sigcomm eBook,
 "Recent Advances in Networking SIGCOMM eBook", Vol.1,
 August 2013.

www.sigcomm.org/content/ebook

My web page

www.maths.adelaide.edu.au/matthew.roughan

Slides available at

/talks.html

Links, and some data and code available

/traffic\_matrices.html

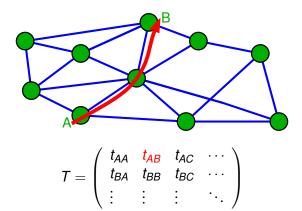
## The Hard Lesson (for me)

- This is a little story about a Boy from the Sticks who went to the Big City and ...
- Queueing Theory wasn't as useful as I thought
  - My PhD was on Queueing Theory (quite a while ago)
  - I went to work at AT&T Labs (which to me was the Mecca of queueing theory) and no-one cared
- Why?
  - unrealistic assumptions
  - not solving a real problem
  - ► lack of data
    - ★ and the data they did have wasn't what you needed
- So it turns out the maths I knew was solving the wrong problem
  - the real problems were actually easier!
  - but less specific, so I had to learn a wider skill base
- A big part revolved around traffic matrices, so here, now live, for one night only ...

## Section 1

Intro

# Traffic Matrix [1]



 $t_{AB}$  is the traffic going from location A to location B across a network

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## **Taxonomy of Traffic Matrices**

- In today's network locations can be
  - physical
    - ★ PoPs = Points of Presence
    - \* routers
    - ★ links
    - servers
  - logical
    - ★ IP addresses
    - common-prefix address blocks (prefixes)
- Offered vs Carried Load
  - Demand vs Traffic matrix
- Ingress-Egress (IE) vs Origin-Destination (OD)

## Offered vs Carried Load

- Offered load is the potential traffic
  - traffic desire network
- Carried load is what we actually see
- They can be different
  - congestion (i.e., capacity constraints reached)
  - feedback (formal or heuristic)
  - non-locality: we observe at a point distant from origin and destination
  - anomalies (e.g., a car crash, link outage, ...)
- It's quite hard to observe offered load so mostly we talk about traffic matrices, not demand matrices

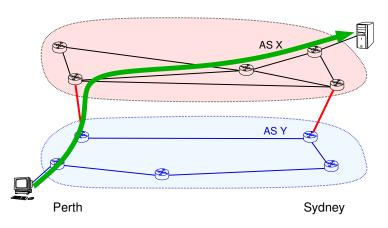
#### **Invariants**

#### Why do these issues really matter?

- What we really want is an invariant
  - under some set of changes to the network, it doesn't change
  - e.g., in optimisation, we want an input that is invariant under changes in the optimisation variables, within the constraints
- We rarely have a true invariant
  - offered load is more useful than carried load
  - even offered loads aren't completely invariant
    - e.g., new roads change housing patterns, and hence traffic
    - ★ e.g., IE traffic matrices

# Hot Potato Routing

dump traffic off your network as fast as possible

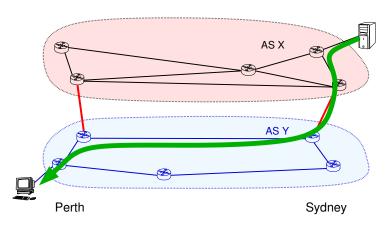


traffic from Perth on AS Y to Sydney on AS X

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## Hot Potato Routing

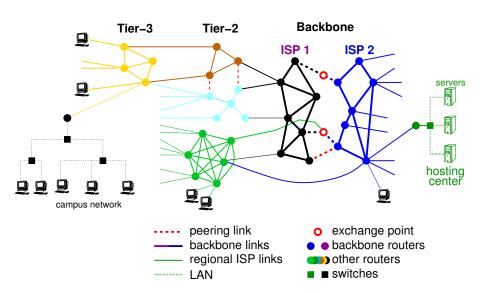
dump traffic off your network as fast as possible



- If I run AS X, all I see is traffic on my network!
  - ▶ IE Traffic Matrices are asymmetric!
  - ▶ IE Traffic Matrices are subject to the whims of routing

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## A Cartoon of the Internet



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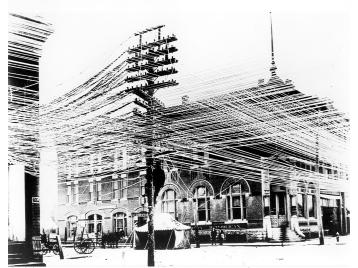
Why do we care about TMs and invariants?



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## Why do we care about TMs and invariants?

Dumb network design (Pratt, Kansas, c1900)



http://www.bellsystemmemorial.com/oldphotos\_6.html

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# **TM Applications**

- Network Operators
  - Network Planning (optimisation)
    - ★ capacity planning (green-fields or incremental)
    - traffic engineering
    - \* ...
  - Network Reliability Analysis
  - Anomaly Detection

These need a **predicted real** traffic matrix

- Researchers
  - Protocol Design
    - e.g., routing protocols
  - Algorithm Design
    - ★ e.g., traffic engineering optimisation algorithms

These need an **ensemble** of **controllable** TMs



## TM Time-line

1937	Telephone Traffic	Kruithof [2, 3]
1960s	Transportation Traffic	e.g., [4]
1996-2000	Network Tomography	Vardi [5], followed by [6, 7]
2000+	Internet Measurement	Feldmann <i>et al.</i> [8, 9]
2002-10	Internet Tomography	Sprint v AT&T
		[10, 11, 12, 13, 14, 15, 16, 17, 18,
2004-10	Anomaly Detection	[22, 23, 24, 25, 20]
2005+	Synthesis	[26, 27]
:		

we'll add some more recent bits towards the end of today's talk

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## **Outline**

- Intro
- 2 How do you get a TM?
- What do TMs look like?
- 4 How do you use a TM?
- 5 What do I do if I don't have any data?

## Section 2

How do you get a TM?

### How to Get Traffic Data

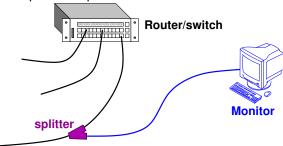
- Packet trace
- SNMP
- Inference (tomography)
- Netflow



#### Packet traces

- tap a link, or router
  - optical, or electronic splitter/coupler

monitoring port



- record every packet's
  - size
  - time (of first byte)
  - headers (IP, TCP, possibly more)

## Data Volume Management

Space is big. You just won't believe how vastly, hugely, mind-bogglingly big it is...

Douglas Adams,

Hitchhiker's Guide to the Galaxy

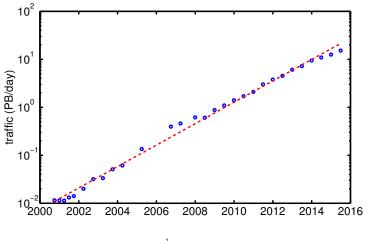
Internet measurement was one of the first real sources of

## **BIG DATA**

- well before the term became trendy
- 10 Gbps link generates 10 Gbps of traffic data (at peak)
  - 2 TB disk is full in less than half an hour
  - and a single 10 Gbps link isn't much today

## Australian Traffic Growth

Doubling every  $\sim$  1.3 years



www.abs.gov.au

# **Data Volume Strategies**

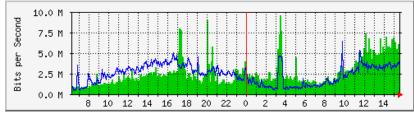
A number of operations can reduce the dataset size

- sampling:
  - standard statistical approach
  - simplest case, sample every Nth packet, or randomly choose 1 in N packets
- **filtering:** only look at packets which meet certain requirements, *e.g.*,
  - only TCP packets
  - only packets between two specific IP addresses
- sketching: (not today)
- aggregation: reduce the granularity of the data somehow
  - aggregate over time, or keys
  - examples: SNMP, Netflow

#### **SNMP**

#### Simple Network Management Protocol

- not just for management
- allows collection of traffic data



- but it's just crude counts
  - no details
  - coarse granularity (e.g., 5 minutes)
  - error prone [28]
  - lots of missing data

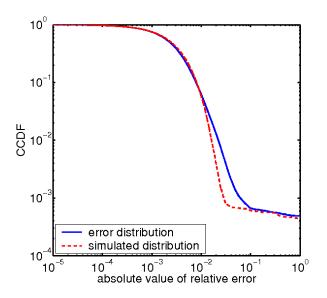


# **Data Quality**

If you think your data is clean, you haven't looked

- numerical errors
  - ALL data has numerical errors
    - our job is not completely remove errors
    - \* calibrate
    - no-one does that well (as yet)
- artifacts
  - the field isn't even a number, e.g., NA
  - numbers in the wrong format, e.g, 1,000 in a CVS file
  - part of a file was overwritten by 2 processes writing to same file
  - a process crashed part way through writing the data
- missing data
  - large number of monitors, some will be offline all the time
- inconsistency
  - two DBs have different information
  - two DBs use different keys for same information
- ambiguous data
  - DB keys don't provide enough information for a task

# Errors in SNMP [28]



# Errors in SNMP [28]

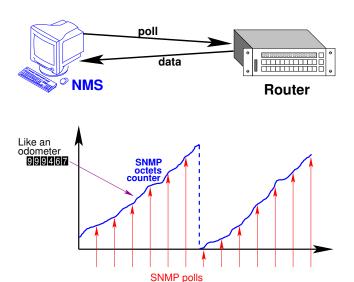
- Most errors are small
- Appears to be a heavy tail for larger errors
- Two main causes of errors
  - simulation is mixture of
    - exponential distribution with mean 0.0035 and probability 0.99882
    - Pareto distribution with cumulative distribution function

$$F(x)=1-\left(\frac{b}{x}\right)^{\alpha},$$

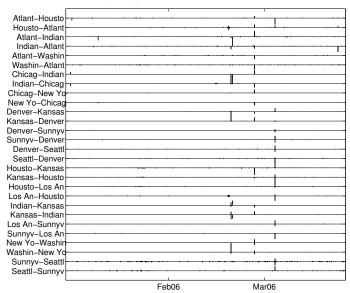
with probability of selection of 0.00118, and parameters  $\alpha =$  0.12 and b = 0.0005.

NB: Pareto component has infinite mean, so need large set of data to observe, and test it

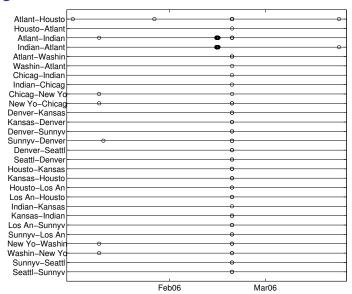
### SNMP data collection



# Errors correlations [28]



## Missing Data in SNMP



## **SNMP** and Traffic Matrices

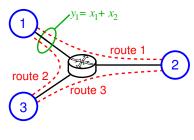
- SNMP contains link counts
  - packets per interface
  - bytes per interface
- No idea where the traffic is going!
  - it doesn't tell you the traffic matrix!

# **Network Tomography**

#### Example

SNMP only gives link counts, not traffic matrices, but they are related

$$y = Rx$$



$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \end{pmatrix} = \begin{pmatrix} 1 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 1 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = R\mathbf{x}$$

# **Network Tomography**

Notes

- Each of the columns of the matrix X are stacked to give a column vector x
- Measurements have errors so

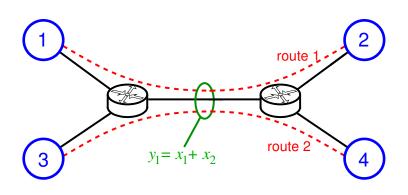
$$y = Rx + z$$

R is not square, so we can't just invert it



# **Network Tomography**

#### **Another Example**



$$y = Rx$$

where R = [1, 1]



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# A Word on Routing Matrices

#### What are they?

- The matrix is an incidence matrix
- ► The matrix is size  $L \times N(N-1)$  where there are L links and N source/destinations in the network
- Simplest form has 0 or 1s
- ▶ A 1 in position (i,j) indicates that route j uses link i, where
- Route i refers to a particular TM source/destination pair
- With load balancing, the matrix might contain fractions
- How do I get one?
  - You need to know your network topology
    - ★ lots of ways to measure this
  - You need to know you network routing, either by
    - measuring current forwarding paths
    - measuring routing policies, and predicting routing

## General Framework

Want to solve the inverse problem

$$y = Rx + z$$

but it's **highly-under-constrained**, so we need **side information** or a **model**, or a **prior**, then we solve via optimisation

$$\operatorname*{argmin}_{\boldsymbol{x}}\|\boldsymbol{y}-R\boldsymbol{x}\|+\lambda d(\boldsymbol{x}_m,\boldsymbol{x})$$

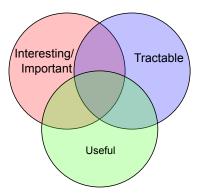
- Note we don't to force the equality because there are measurement errors
- General strategy is called regularisation
- Lots of different possible models
- $\lambda$  lets you trade off between the distance  $d(\cdot, \cdot)$  from the prior model  $\mathbf{x}_m$  and the data  $\mathbf{y}$
- You can use different norms | · | and distances

# **Network Tomography**

Given stacked TM x and routing matrix R, the link loads on the network are given by y which can be written simply as

$$y = Rx + z$$

- lots research [10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21],...
- why so much?



# Why did TM Inference die out as a research topic?

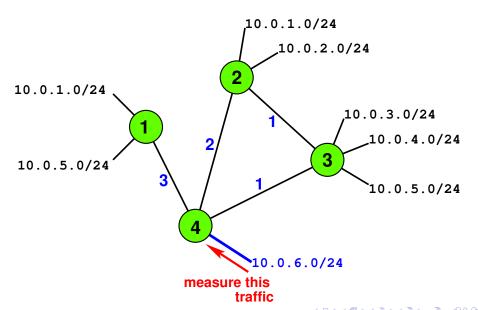
- 2 sorts of data so far
  - packet trace too hard to collect
  - SNMP easy to collect, but hard to use
- There is a third sort: Netflow
  - it's been around for quite a while
  - but it wasn't very easy to collect until more recently

## Netflow (Cisco v5)

- Idea: aggregate to close approximation of a TCP connection
  - keep one record per flow
  - key 5-tuple: IP source, dest, protocol and TCP source, dest port
  - also
    - ★ localise in time (but complicated)
    - ★ per Ingress interface
    - ★ IP ToS
  - store
    - ★ counters for packets and bytes
    - ★ TCP flags
    - start and stop times
    - a little about routing
- Practicality: aggregate by key
  - flush records using
    - ★ timeout, O(15 seconds), (to separate similar connections, e.g., DNS)
    - ★ when flow record cache is full
    - ★ every X minutes, O(15 minutes), (stop staleness of records)
  - not bi-directional



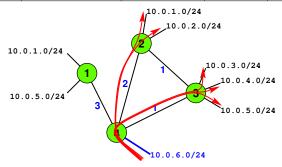
## Netflow example application



## Example traffic matrix computation

### Measured incoming traffic at node 4

ingress node	source prefix	dest prefix	volume	egress node
4	10.0.6.0/24	10.0.1.0/24	10	2
4	10.0.6.0/24	10.0.2.0/24	11	2
4	10.0.6.0/24	10.0.3.0/24	21	3
4	10.0.6.0/24	10.0.4.0/24	6	3
4	10.0.6.0/24	10.0.5.0/24	3	3

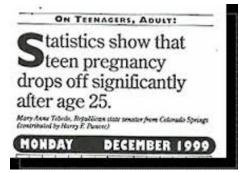


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#### **Netflow TM**

#### Netflow can be used to construct a TM

- but you need more data than you think (e.g., topology)
- Netflow isn't universal historically poor vendor support
- have to sample
  - but almost everyone is hopeless at statistics



• What do the errors in Netflow look like?

## Section 3

What do TMs look like?

- A TM really has three dimensions
  - 2 spatial: origin and destination
  - ▶ 1 temporal: time of each snapshot

so we could represent it as a tensor

- We usually use a matrix, but it could mean
  - a purely spatial snapshot at a particular time
  - a matrix of stacked vector snapshots

$$X = \left[\begin{array}{c|c} \vdots & \vdots & & \vdots \\ \boldsymbol{x}_1 & \boldsymbol{x}_2 & \cdots & \boldsymbol{x}_t \\ \vdots & \vdots & & \vdots \end{array}\right]$$
time

- Could have other dimensions
  - traffic types



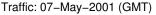
- A TM could contain
  - number of flows
  - number of packets
  - number of bytes

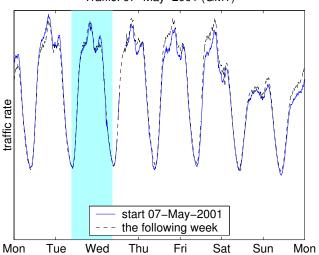
Mostly they give bytes

- A TM snapshot is usually an average of some time interval Common examples are
  - 5 minutes
  - 30 minutes

Temporal patterns

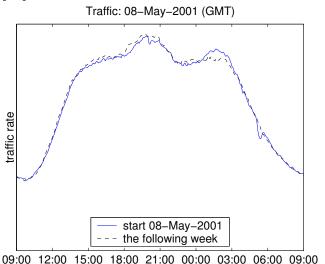
Large ISP [29] local traffic





#### Temporal patterns

Large ISP [29] local traffic



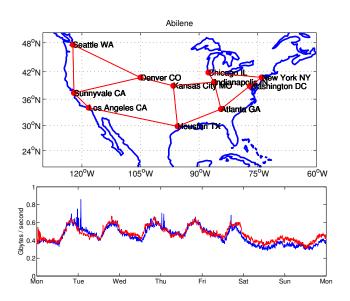
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time (GMT)

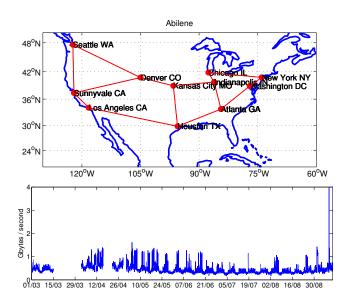
# Individuals are random, but the flock is not!



## Examples: Abilene c2004



## Examples: Abilene c2004



## Temporal pattern

$$x(t) = m(t) + \sqrt{am(t)}W(t) + I(t),$$

where

$$m(t) = S(t) L(t)$$

and

- L(t), long-term traffic trend

- $\bullet$  I(t), anomaly component
- o a, peakedness



### Model rationale

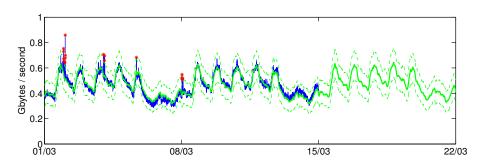
- Period pattern is well known, 24 hours, 1 week
- Multiplexing

$$x_{\text{agg}}(t) = \sum_{i=1}^{K} m_i(t) + \sum_{i=1}^{K} \sqrt{a_i m_i(t)} W_i(t) + \sum_{i=1}^{K} I_i(t).$$

- leads to consistent mean and variance estimates
- Presumption is that growth arises mainly from new sources, not increases in old sources
  - NB: source here might not mean individuals
- It's an easy model to estimate



## Data and model





#### Spatial patterns

	dst										l		
src	1	2	3	4	5	6	7	8	9	10	11	12	sum
1	0.07	0.07	0.43	0.00	0.06	0.12	0.06	0.00	0.05	0.00	0.00	0.25	1.12
2	0.00	4.09	6.42	0.06	7.07	4.42	1.59	0.02	3.24	0.03	0.16	11.09	38.18
3	0.00	4.70	25.48	4.11	13.99	11.53	3.31	87.27	5.22	0.01	0.08	7.70	163.38
4	0.00	1.93	10.25	1.68	5.63	6.11	2.59	0.01	4.11	2.60	0.04	5.92	40.88
5	0.00	4.76	0.25	0.01	24.06	0.04	0.01	0.02	1.24	0.02	0.03	18.05	48.49
6	0.00	2.87	23.73	1.55	13.53	4.78	2.89	0.01	9.45	0.08	0.50	7.64	67.02
7	0.00	0.67	4.79	1.92	3.50	2.24	1.25	0.00	0.93	0.02	0.03	3.31	18.67
8	0.00	4.18	2.58	5.80	26.35	0.17	0.16	1.41	10.88	2.11	3.64	16.67	73.97
9	0.00	8.61	12.34	5.71	18.21	11.05	3.84	0.41	36.36	0.02	0.52	17.31	114.37
10	0.00	0.18	0.04	1.71	1.69	0.00	0.06	5.61	0.96	1.82	8.44	0.36	20.86
11	0.00	3.47	3.28	0.54	8.60	0.13	0.93	3.92	1.77	0.81	0.61	2.32	26.38
12	0.00	18.20	16.04	0.83	34.03	11.18	5.64	0.09	25.57	0.08	0.80	47.02	159.47
sum	0.07	53.74	105.61	23.94	156.73	51.76	22.34	98.77	99.77	7.59	14.84	137.65	772.80

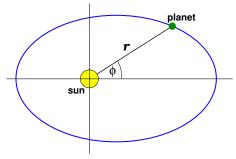
Abilene 5 minute traffic matrix from April 15th, 2004 from 16:25-16:30, in Mbps.

#### Spatial patterns

Newtonian gravity

$$F=\frac{GMm}{r^2}$$

- force depends on mass and distance
- no dependence on type of mass
  - ★ lead has the same gravitational constant as air





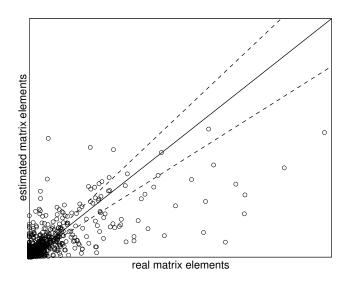
# Simple Gravity Model

Internet traffic model:

$$T(i,j) = \frac{T_{\text{in}}(i) \times T_{\text{out}}(j)}{T_{\text{total}}}$$

- traffic between i and j only depends on how "big" i and j are
  - no dependence on the type of location
- different from Newtonian gravity
  - no distance term
- not a perfect model, but it's useful

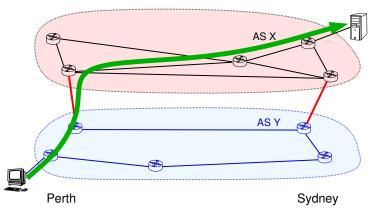
## Errors in gravity model [11]



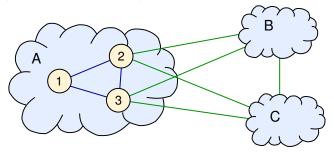
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# Hot Potato Routing and Gravity Models

We model OD TMs, but see IE TMs

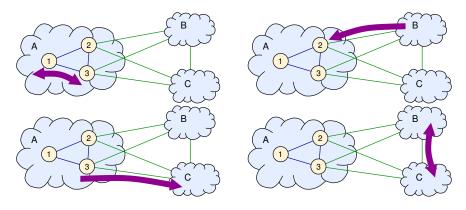


Simple Example with 3 Autonomous Systems

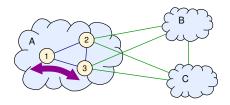


(uniform) gravity model OD traffic matrix

#### There are four classes of flows:

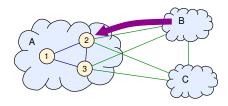


each behaves differently.



We only observe IE TM, which is made up of three components

$$X_{\text{internal}}^{(IE)} = \begin{array}{c} 1 & 2 & 3 \\ 1 & 1/9 & 1/9 & 1/9 \\ 2 & 1/9 & 1/9 & 1/9 \\ 3 & 1/9 & 1/9 & 1/9 \end{array}$$

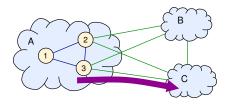


We only observe IE TM, which is made up of three components

$$X_{\text{arriving}}^{(IE)} = egin{arrivin} 1 & 2 & 3 \\ 1 & 0 & 0 & 0 \\ 2 & 1/3 & 1/3 & 1/3 \\ 3 & 1/3 & 1/3 & 1/3 \end{pmatrix}$$

 assumes traffic from B and C is split evenly over possible entry points (routers 1 and 2)

◄□▶
□▶
4□▶
4□▶
4□▶
4□▶
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We only observe IE TM, which is made up of three components

$$X_{\text{departing}}^{(IE)} = \begin{array}{ccc} & 1 & 2 & 3 \\ & 1 & 0 & 1/3 & 1/3 \\ & 2 & 0 & 2/3 & 0 \\ & 3 & 0 & 0 & 2/3 \end{array}$$

- assumes hot potato routing
- internal IGP weights are equal



Total IE traffic matrix

$$X^{(IE)} = \begin{pmatrix} 1/9 & 4/9 & 4/9 \\ 4/9 & 10/9 & 4/9 \\ 4/9 & 4/9 & 10/9 \end{pmatrix}$$

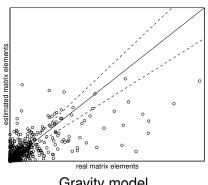
which is far from fitting the gravity model,

$$X_{\text{gravity}}^{(IE)} = \begin{pmatrix} 1/5 & 2/5 & 2/5 \\ 2/5 & 4/5 & 4/5 \\ 2/5 & 4/5 & 4/5 \end{pmatrix}$$

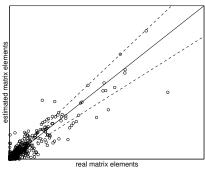
even though all of its OD components do fit the gravity model

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# Generalised Gravity Model Errors



Gravity model



Generalised Gravity Model

# In general

There are lots of complexities not included in the gravity model

- IE matrices not symmetric
- Diagonal entries are always a problem
- People aren't sheep
- new(ish) tech: CDNs, clouds, ...

We could start down a long road of modelling here, which I don't want to do just yet, but note that tomographic techniques fix some of the errors using link data.

# In general

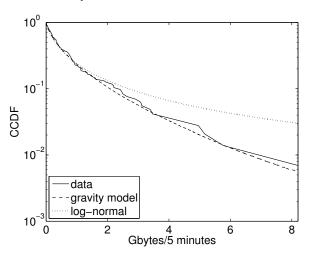
There are lots of complexities not included in the gravity model

- IE matrices not symmetric
- Diagonal entries are always a problem
- People aren't sheep
  - Australians aren't New Zealanders
- new(ish) tech: CDNs, clouds, ...

We could start down a long road of modelling here, which I don't want to do just yet, but note that tomographic techniques fix some of the errors using link data.

## Distributional properties [27]

TM entries are not heavy tailed



NB: here the gravity model is formed from row/col sums that are drawn from an exponential distribution (more on this later)

### Section 4

How do you use a TM?

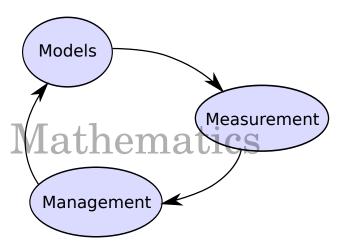
# **Network Management**

Network management, as defined by the OSI [30] FCAPS

- F Fault recognise, isolate, correct, prevent faults
- C Configuration programming a set of flexible devices (switches, routers, and servers) to implement the high-level goals of the network operator
- A Accounting gather usage statistics of users primarily for billing
- Performance ensure network performance remains at "acceptable" levels
- S Security ensure availability, integrity, confidentiality But also faults, and accounting ...

### $NM^4$

Network Management is an **integrated process** not a set of tasks





# Network engineering goals

Reliability



- Reliability
- Reliability

- Reliability
- Reliability
- Cost

- Reliability
- Reliability
- Cost
- Performance

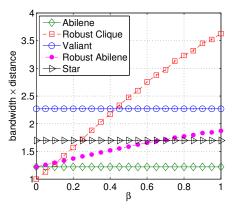
- Reliability
- Reliability
- Cost
- Performance
- Reliability

#### Network Reliability Analysis

- Answer "what if?" questions
  - what if link X fails?
- It's not just about connectivity
  - rerouted traffic can cause congestion
- To do this we need
  - network configuration
  - fault risks
  - traffic data
  - performance models
- An example

#### Some interesting bits

All TMs have errors – how does that affect answers?



Some methods (of network design) are highly-sensitive to errors, and others aren't!!! [31] (2014)

analysis required ability to generate variations around a TM

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#### Other Applications for Network Operators

#### Usually involve prediction of TMs, though over different horizons

- Network planning
  - 6 months to a year: planning capacity
  - 1 day to 2 weeks: traffic engineering
- Detecting unusual traffic (anomaly detection)
  - minutes to hours

#### Synthesis – the next challenge

- Network operators design based on "real" TMs
  - now there are various methods to get the required data
  - need to be able to work with errors
  - synthesis can help [31]
- Researchers need data as well
  - but network operators don't release TM data
  - even if they did, they would never release enough
    - ★ e.g., to do stats on results
  - even if they did provide enough, researchers need control
    - e.g., to extrapolate results

So where do we (the research community) get TM data?

#### Section 5

What do I do if I don't have any data?

## Pop quiz

If you choose an answer to this question at random, what is the chance you will be correct?

- A 25%
- B 50%
- C 66%
- D 25%

#### Specific Applications for Researchers

#### Usually involve an *ensemble* of traffic matrices

- Designing a new
  - routing protocol
- Testing algorithms for
  - anomaly detection
  - traffic engineering or network planning
- Synthesising networks
  - traffic is a fundamental input [32, 33]

Could also apply for green-fields planning

## Data is hard to get

- Network operators don't share
  - traffic data is proprietary
  - traffic data is private
- How representative is any set anyway?
  - Abilene might be thought outdated
- We need lots of data for some tasks
  - e.g., anomaly detection needs to estimate small probabilities [34]
  - more than you get from one network
- We might need data where there is no network
  - green-fields planning
  - what happens when my network scales up × 10?

Synthesis saves the day!

#### Reproducible research

An article about computational science in a scientific publication is not the scholarship itself, it is merely advertising of the scholarship. The actual scholarship is the complete software development environment and the complete set of instructions which generated the Figures.

Buckheit and Donoho [35]

- Some Internet data can never be shared
- Too much Internet research is NOT reproducible
  - this stifles science
  - it results (sometimes) in incorrect results
  - it encourages fraud and other scientific malfeasance
- Synthesis provides a (partial) solution



#### Synthesis Requirements: SCERC

#### Simplicity:

- Occam's razor
- Principle of parsimony
- Bonini's paradox

Everything simple is false.

Everything which is complex is unusable.

Paul Valéry

- Control: test methods against assumptions.
- Efficiency: TMs can be big, plus we want to generate many.
- Realism: simplest to think you understand, hardest to really understand!
- Consistency: allow apples to apples comparisons

#### Synthesis formalities

- We want to generate an ensemble
  - collection of instances with some probability measure
  - need to have controlled statistical variation there is no point in making all instances the same!
- Want to incorporate some knowledge or assumptions
  - maybe because we have some data
  - maybe because we want to compare our results to someone elses'
- Don't want extraneous, unstated assumptions

#### The answer is synthesis (or simulation)

- The question is, using what model?
- I have a few answers, and they go in the order

 $\begin{array}{c} \text{Simple} \\ \Downarrow \\ \text{Complex} \\ \Downarrow \\ \text{Simple} \end{array}$ 

#### Simple again

- What if we started with a set of "axioms"
  - things we know about a set of traffic matrices
  - ensemble properties
- How would we build models that
  - include the parts we want
  - don't accidentally include other assumptions

## Simple again

- What if we started with a set of "axioms"
  - things we know about a set of traffic matrices
  - ensemble properties
- How would we build models that
  - include the parts we want
  - don't accidentally include other assumptions
- Maximum entropy [36]
  - ► Maximum entropy ⇒ gravity-like models
  - ▶ We have code https://github.com/ptuls/MaxEntTM

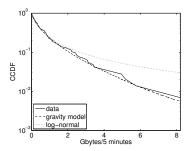
#### **Simple**

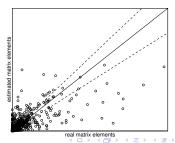
#### Use the gravity model [27]

- Generate random row and column sums
  - exponential random variables seemed to work
- Calculate the gravity model
  - it's just multiplication
- Possibly scale to match required total

#### Simple

- Pros
  - very simple
  - matches distribution well
- Cons
  - structure isn't right
  - lack of control





#### Complex

You can think of any number of ways to include more complex models, ideas, assumptions, ....

#### Challenges

- Loose simplicity
- Loose efficiency
- Testing realism
- In theory you gain control, but in practice you often end up with many parameters which are hard to estimate (from data), or guess by other means

## Simple again

- What if we started with a set of "axioms"
  - things we know about a set of traffic matrices
  - ensemble properties
- How would we build models that
  - include the parts we want
  - don't accidently include other assumptions

## Simple again

- What if we started with a set of "axioms"
  - things we know about a set of traffic matrices
  - ensemble properties
- How would we build models that
  - include the parts we want
  - don't accidently include other assumptions
- Maximum entropy does this [36]

## Maximum Entropy Idea [37]

Shannon entropy

$$H(X) = -\sum_{x} p(x) \log p(x),$$

can be seen as a measure of how much information we need to describe X

- Another way to say that is it's a measure of uncertainty
- If we find a distribution of X that maximises H(X) subject to any constraints, it must be the one that imposes the least possible a priori assumptions or knowledge on X
- Find p(x) is just an optimisation problem



#### Simple Case

Imagine we knew certain features of the data

$$\mathbb{E}ig[\sum_{j} X_{i,j}ig] = r$$
 (outgoing)
 $\mathbb{E}ig[\sum_{i} X_{i,j}ig] = c$  (incoming)
 $\mathbb{E}ig[\sum_{i,j} X_{i,j}ig] = T$  (total)
 $\sum_{i} r_i = \sum_{j} c_j = T$  (consistency)

Then the natural MaxEnt model is a gravity model

$$X = T \underbrace{U}_{\text{row column}} \underbrace{V}^T$$

where *U* and *V* are vectors of independent exponential random variables whose average matches the row and col sums.

This is (almost) the gravity model proposed earlier!

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#### More complex cases

- Spatio-temporal structure
- Constraints on variance (e.g., errors in measurements)
- Soft v hard constraints
- Convex constraints

Works in a very modular, building-block manner

# Finding the maximum entropy distribution $\neq$ sampling from it

- Simple cases have closed forms, i.e., are easy
- More complex cases we need to use a sampling algorithm
  - e.g., MCMC (Markov Chain Monte Carlo)
- These aren't always tractable without some care!
  - we have reasonable code for common TM cases https://github.com/ptuls/MaxEntTM

#### Other plusses

- Maximum entropy creates a matrix between
  - assumptions
  - models
- We see this with gravity model
  - now we know why it is a good model to start with, and when it is good, and when it is bad
- (truncated) normal implies mean and variance

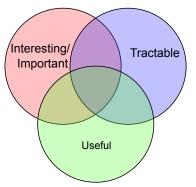
## Recap

- Intro
- 2 How do you get a TM?
- What do TMs look like?
- 4 How do you use a TM?
- 5 What do I do if I don't have any data?

#### Conclusion

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 network performance shouldn't be considered without thinking about the data/measurements we can have, and the tasks at hand



- connecting research to real problems is
  - necessary if you want to have impact
  - rewarding, because useful problems are often interesting

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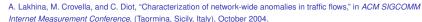


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## Bonus frames